

# Symbolic Verification of Distance-bounding Protocols

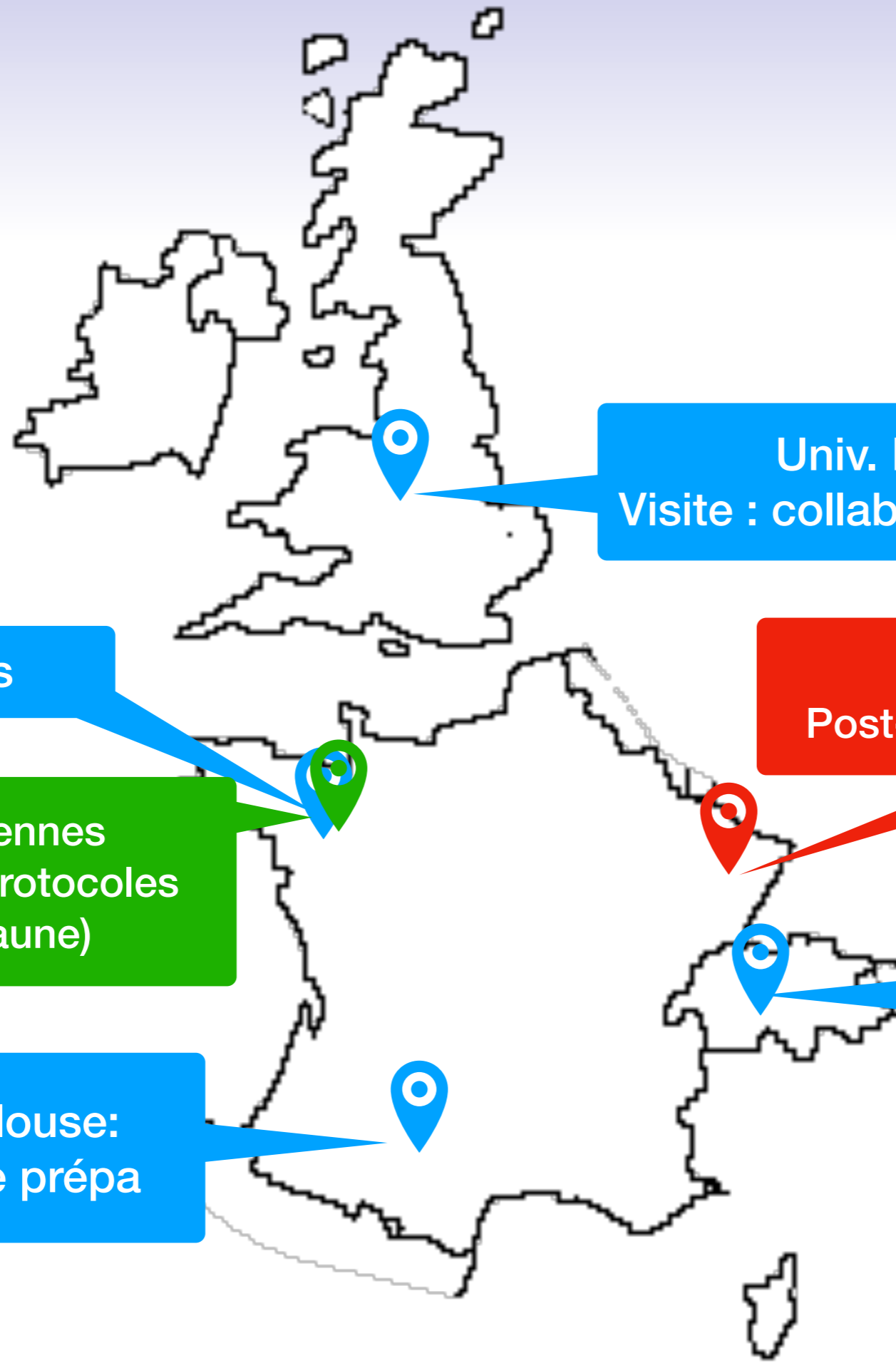
*Application to payments protocols*

**Alexandre Debant**

*Université de Lorraine, CNRS, Inria, LORIA,*

**Seminar at LIRMM  
February 12<sup>th</sup> 2021**





Univ. Birmingham  
Visite : collab. avec Tom Chothia

ENS Rennes

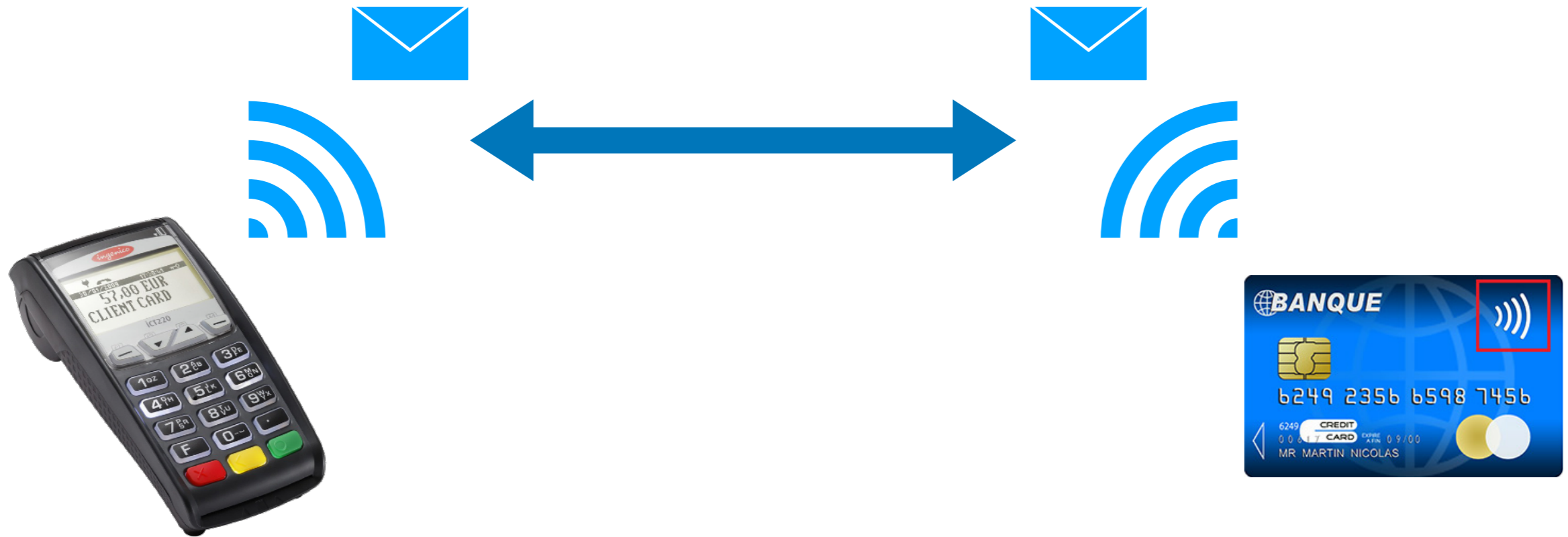
INRIA Nancy  
Post-doc avec Véronique Cortier

IRISA - INRIA Rennes  
Thèse : preuve de protocoles  
(Stéphanie Delaune)

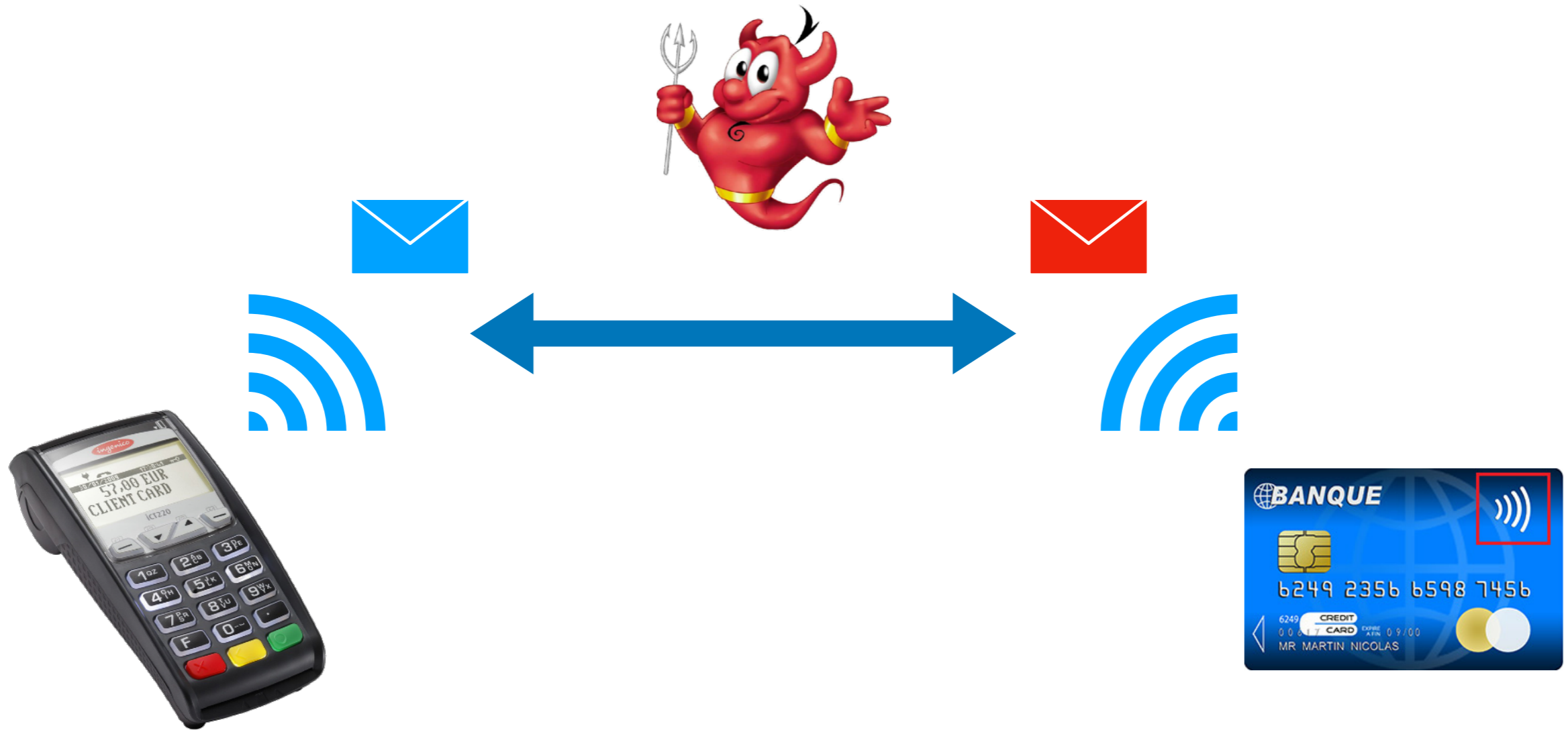
EPFL  
Stage : preuve de  
programmes Scala  
(Viktor Kuncak)

Auch + Toulouse:  
Bac + classe prépa

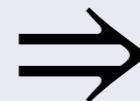
# Introduction



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**Sensitive data  
+ wireless communications**



**risks of attacks**

# Many applications



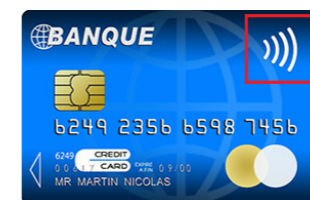
**Passport**



**Wi-Fi**



**Transport  
ticketing**



**Credit card**

# Many applications that are insecure....



[Chothia *et al.* - 2010]

**Passport**



[Vanhoef *et al.* - 2017]

**Wi-Fi**



[Nohl *et al.* - 2008]

**Transport  
ticketing**



[Murdoch *et al.* - 2010]

**Credit card**

# Cryptographic protocols

## Cryptographic primitives



encryption/decryption



digital signature

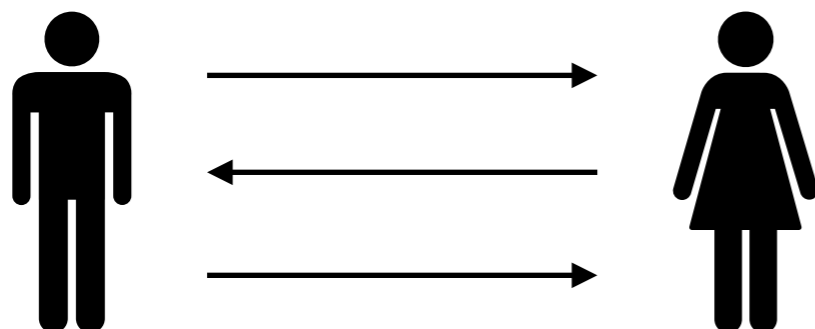


hash function



zero-knowledge proof

**Protocols** - how messages are exchanged?



# Cryptographic protocols

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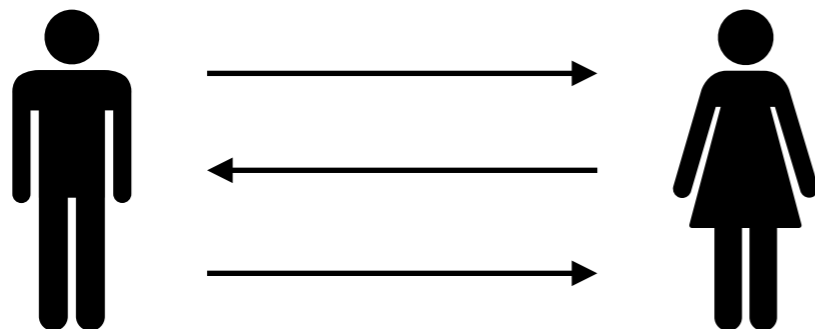


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zero-knowledge proof

**Protocols** - how messages are exchanged?



**Cryptography is useless  
if misused!**



# Two major families of models...

... with some **advantages** and some **drawbacks**.

## Computational models

- + messages are bitstrings, a general and powerful attacker
- tedious proofs, sometimes mechanized, but often hand-written



## Symbolic models

- Some abstractions (messages, attacker...)
- + procedures and automated tools



Some results make a link between these two models  
[Abadi & Rogaway - 2000]

# Symbolic verification in a nutshell

## Messages

- Function symbols:  $\text{enc}(x, k)$ ,  $\text{sign}(x, k)$ ,  $h(x)$ ,...
- Equations:  $\text{dec}(\text{enc}(x, k), k) = x$

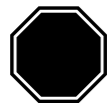
## Protocols

- Process algebra, multiset rewriting rules, Horn clauses...

## The attacker can...



read / overwrite messages



intercept / block messages

## The attacker cannot...



break crypto



use side-channels

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**Perfect cryptography**

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# Existing verification tools

## Bounded number of sessions

- ▶ **decidable** for classes of protocols
- ▶ tools implement decision procedures



AKiSs

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## Unbounded number of sessions

- ▶ **undecidable** in general
- ▶ efficient tools in practice but:
  - ▶ do some approximations
  - ▶ may not terminate

ProVerif



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ProVerif



5G-AKA

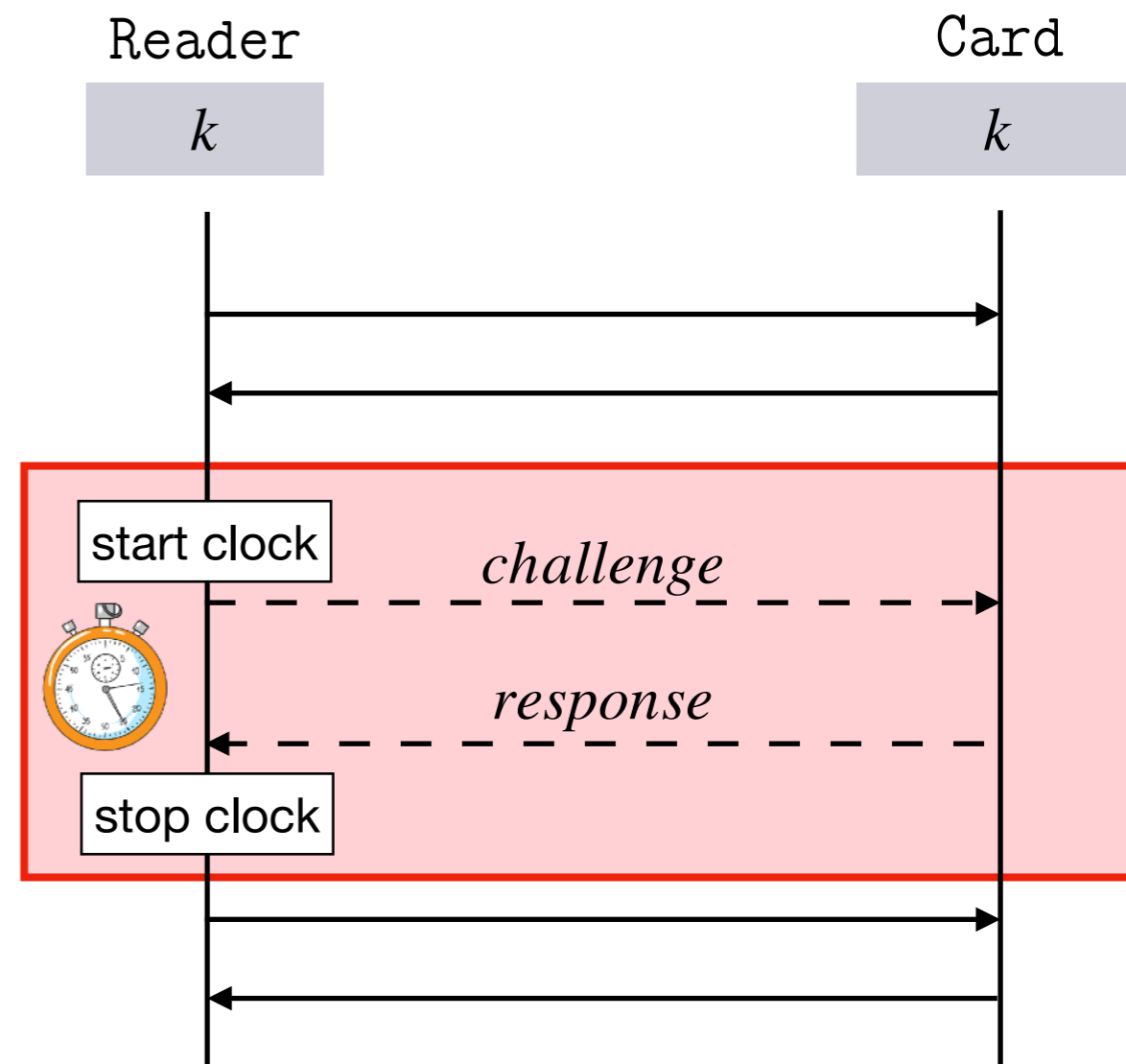


Belenios e-voting

# Proving the physical proximity

## History of distance-bounding protocols

- **First:** Brands and Chaum protocol (1993)
- **Today:** more than 40 new protocols since 2003
- **Application:** in EMV's specification since 2016



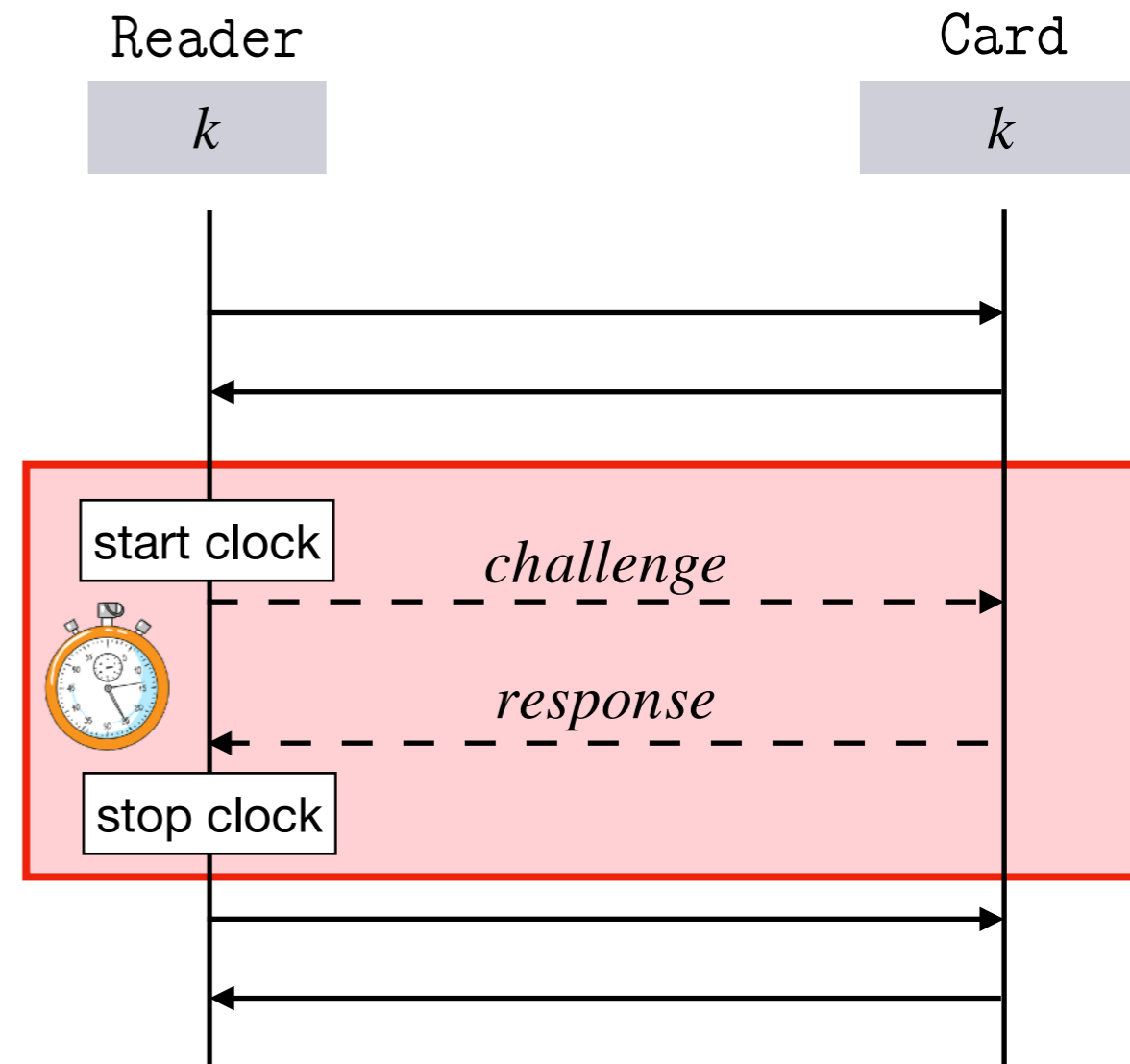
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- Standard models and tools: do not model time and locations!
  - Main specific models:
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- ➔ no automated verification procedure...





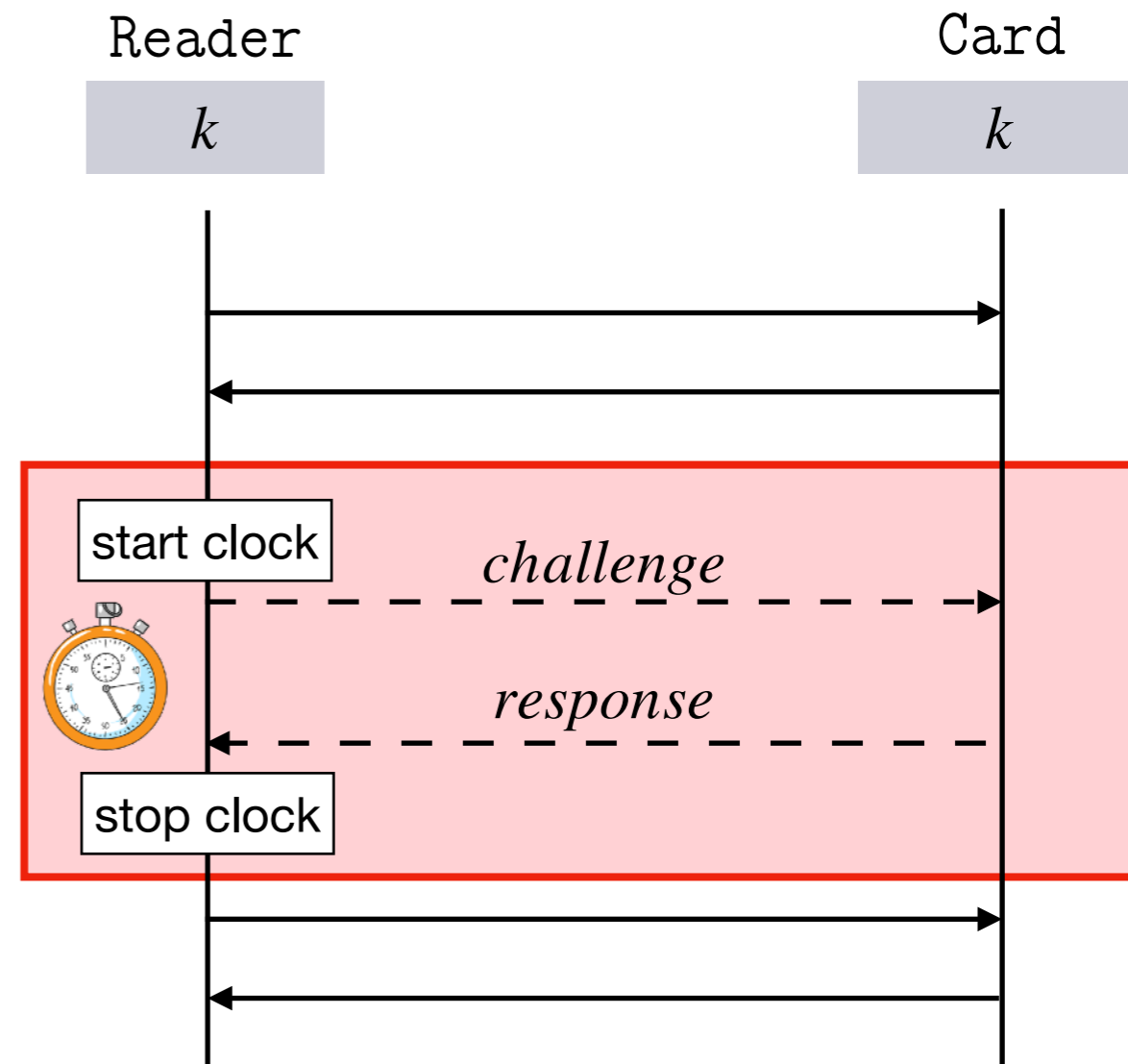
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Can we design a framework that allows for a **fully automated** verification?

# The story of verification

Symbolic model

1. **Syntax and semantics** for describing protocols
2. Formally define the **security properties**

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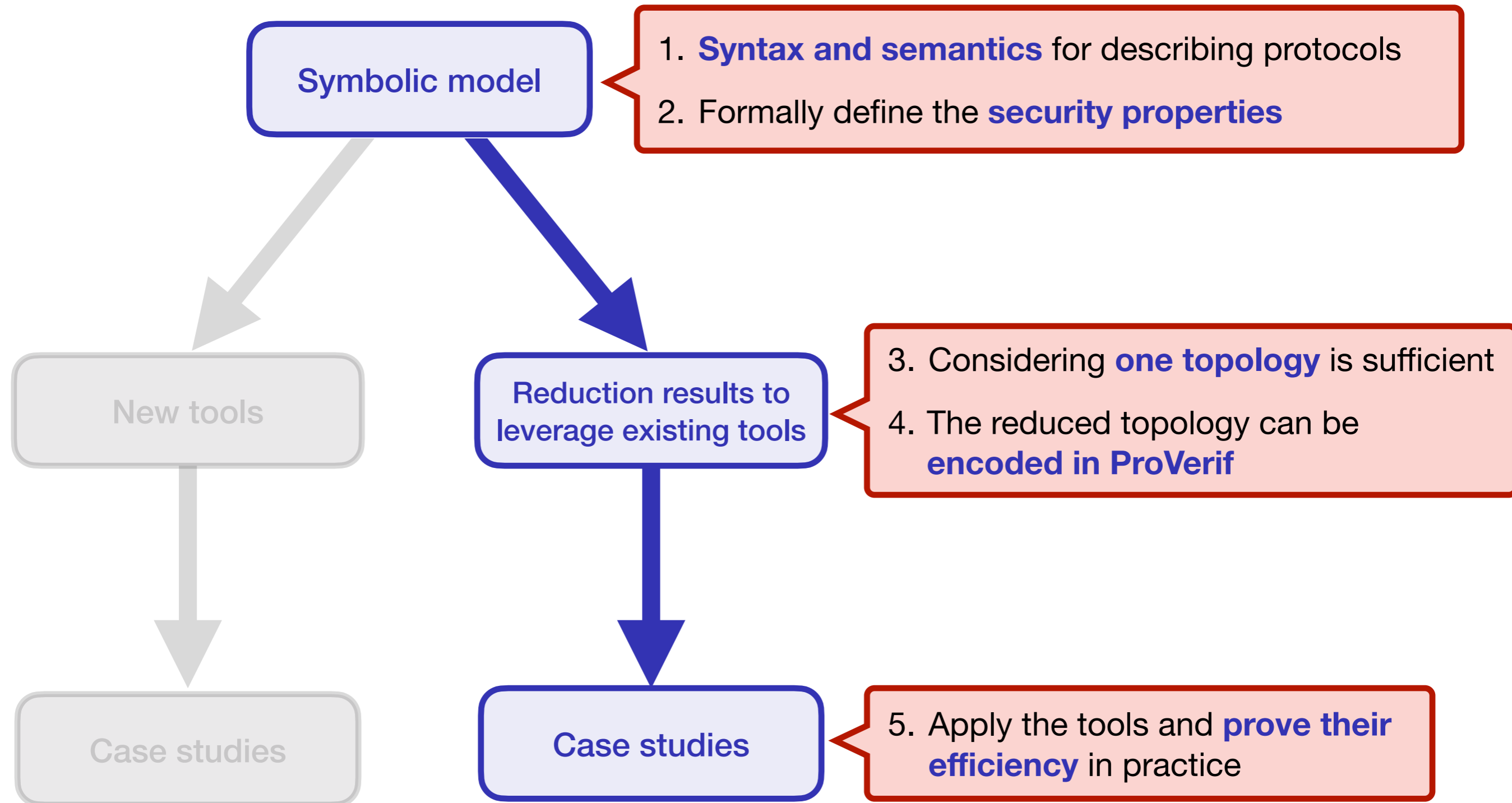
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New tools

Reduction results to leverage existing tools

3. Considering **one topology** is sufficient
4. The reduced topology can be **encoded in ProVerif**

# The story of verification



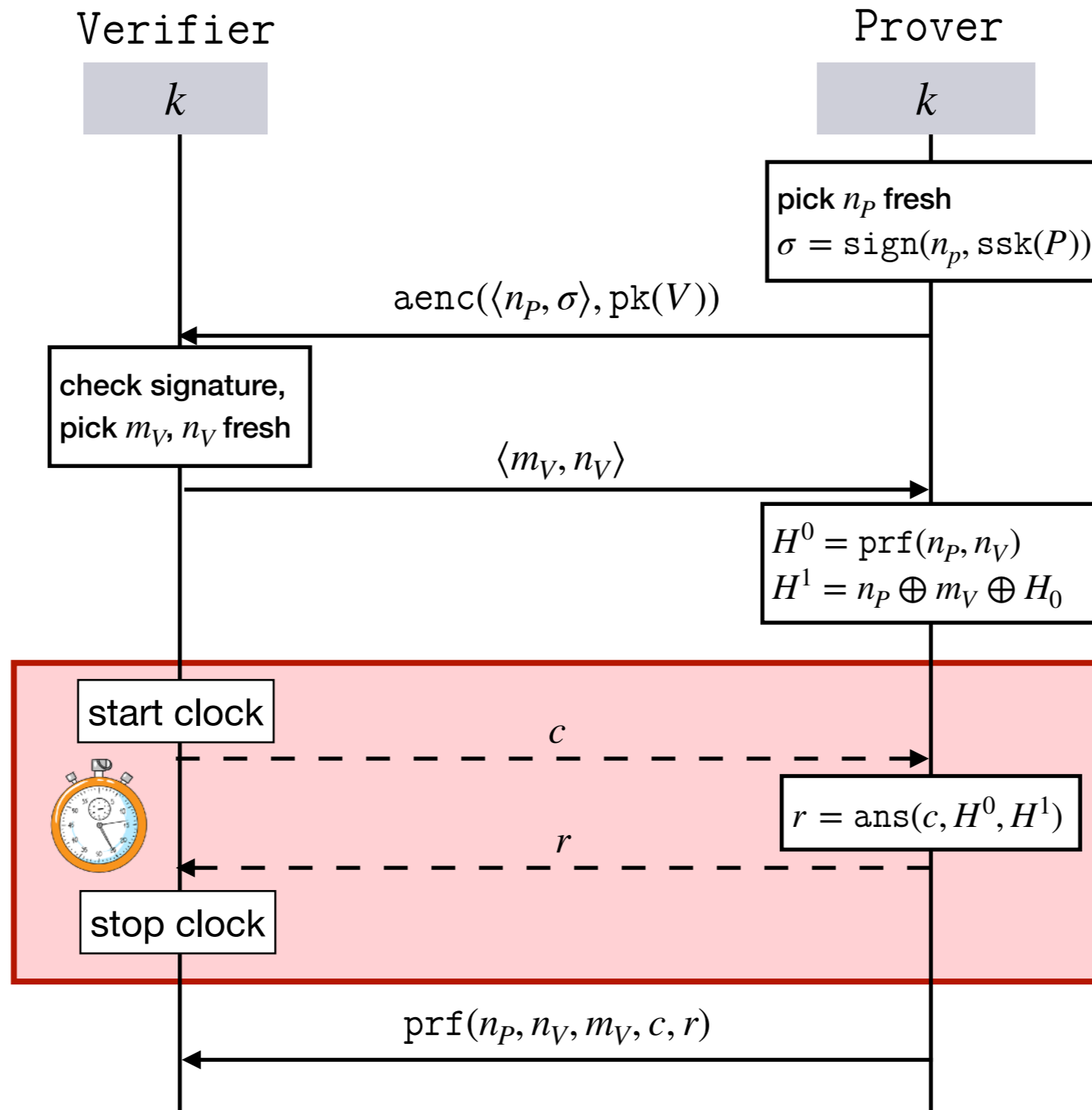
**A symbolic model  
with time and locations**

---

syntax and semantics

# SPADE

[Bultel et al. - 2016]





# Term algebra



**Messages:** terms built over a set of **names**  $\mathcal{N}$  and a **signature**  $\Sigma$  given with either an **equational theory**  $\mathbb{E}$  or a **rewriting system**.

## Example

- ▶ **Function symbols:** `aenc`, `adec`, `pk`, `sk`, `sign`, `get_message`, `spk`, `ssk`,  $\langle \cdot, \cdot \rangle$ , `proj1`, `proj2`

- ▶ **Rules:**

`adec(aenc(x, pk(y)), sk(y)) → x`

`get_message(sign(x, ssk(y)), spk(y)) → x`

`eq(x, x) → ok`

`proj1(⟨x, y⟩) → x`

`proj2(⟨x, y⟩) → y`

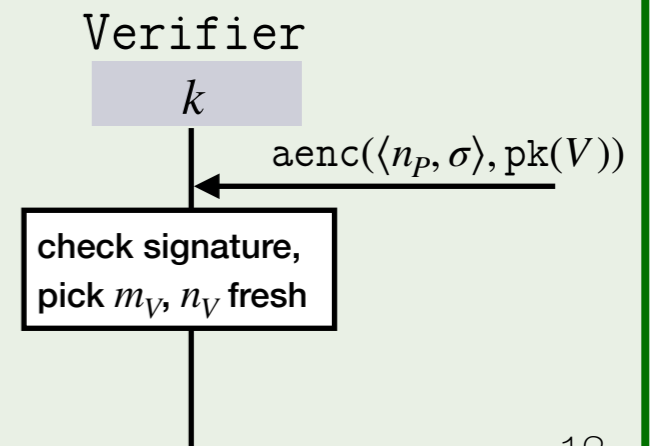
## Running example

`V(v, p) = in(x).`

`let u = adec(x, sk(v)) in`

`let xok = eq(proj1(u), get_message(proj2(u), spk(P))) in`

`...`



# Process algebra

The role of each agent is described by a process following the grammar:

$P$	$:=$	$0$	null process
		$\text{new } n . P$	name restriction
		$\text{let } x = u \text{ in } P$	conditional declaration
		$\text{out}(u) . P$	output
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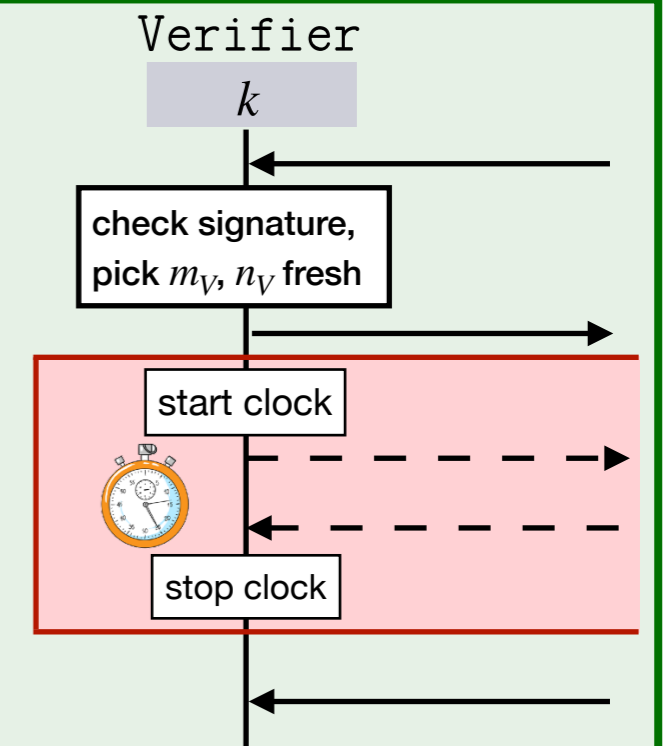
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   $\text{new } m_V . \text{new } n_V .$   
   $\text{out}(\langle m_V, n_V \rangle) .$   
   $\text{reset} . \text{new } c . \text{out}(c) . \text{in}^{<t}(y) .$   
   $\text{in}(z) \dots$ 
```



# Semantics

## Physical restrictions

- ▶ **locations:** elements in  $\mathbb{R}^3$ , i.e.  $\text{Loc} : \mathcal{A} \rightarrow \mathbb{R}^3$
- ▶ **distance:** Euclidean norm between locations, i.e.  $\text{Dist}(a, b) = \frac{\|\text{Loc}(a) - \text{Loc}(b)\|}{c}$
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## System configuration $(\mathcal{P}, \Phi, t)$

- ▶  $\mathcal{P}$ : multiset of processes which remain to execute, i.e.
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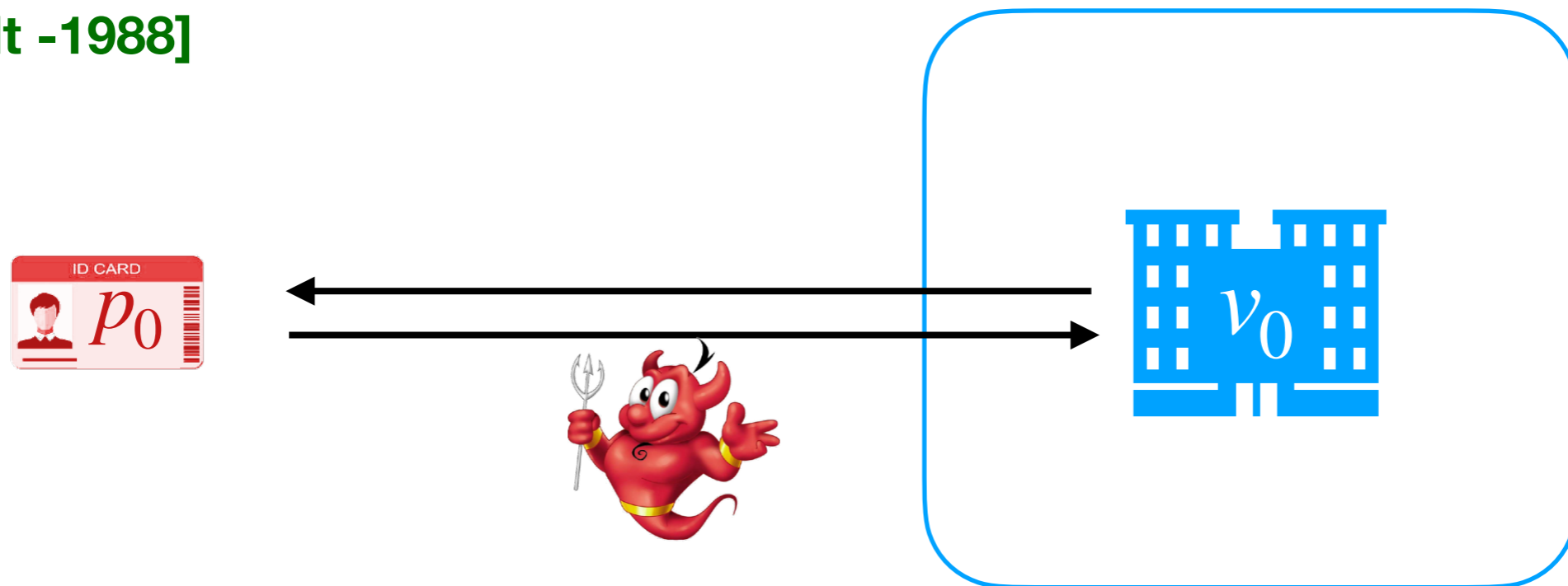
## Execution rules

- ▶ **TIM:**  $(\mathcal{P}, \Phi, t) \longrightarrow (\text{Shift}(\mathcal{P}, \delta), \Phi, t + \delta)$  with  $\delta > 0$
- ▶ **OUT:**  $([\text{out}(u) . P]_a^{t_a} \uplus \mathcal{P}, \Phi, t) \xrightarrow{a, \text{out}(u)} ([P]_a^{t_a} \uplus \mathcal{P}, \Phi \cup \{w \xrightarrow{a, t} u\}, t)$
- ▶ **IN:**  $([\text{in}(x) . P]_a^{t_a} \uplus \mathcal{P}, \Phi, t) \xrightarrow{a, \text{in}(u)} ([P\{x \mapsto u\}]_a^{t_a} \uplus \mathcal{P}, \Phi, t)$   
if  $u$  is deducible from  $\Phi$  **at time  $t$**
- ▶ ...

# Distance fraud/hijacking attack

An **honest verifier** shall not authenticate a **malicious and distant prover**

[Desmedt -1988]

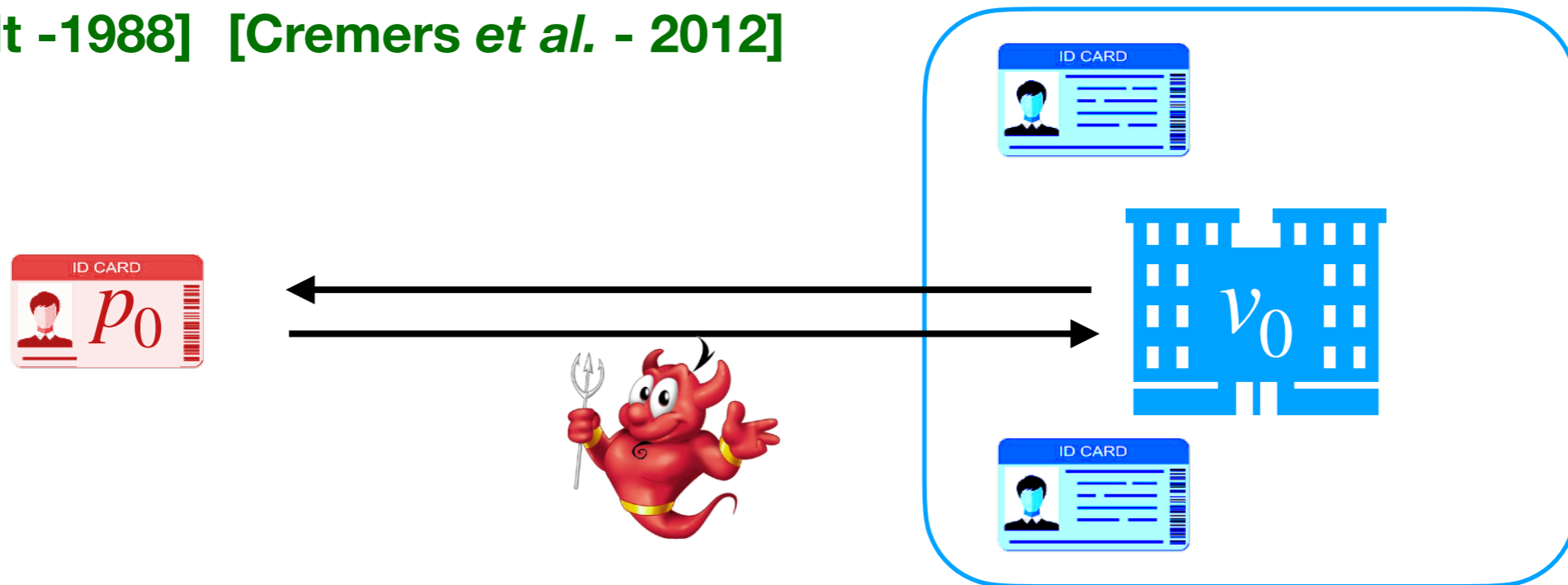




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An **honest verifier** shall not authenticate a **malicious and distant prover** even in the presence of **honest participants** in his vicinity.

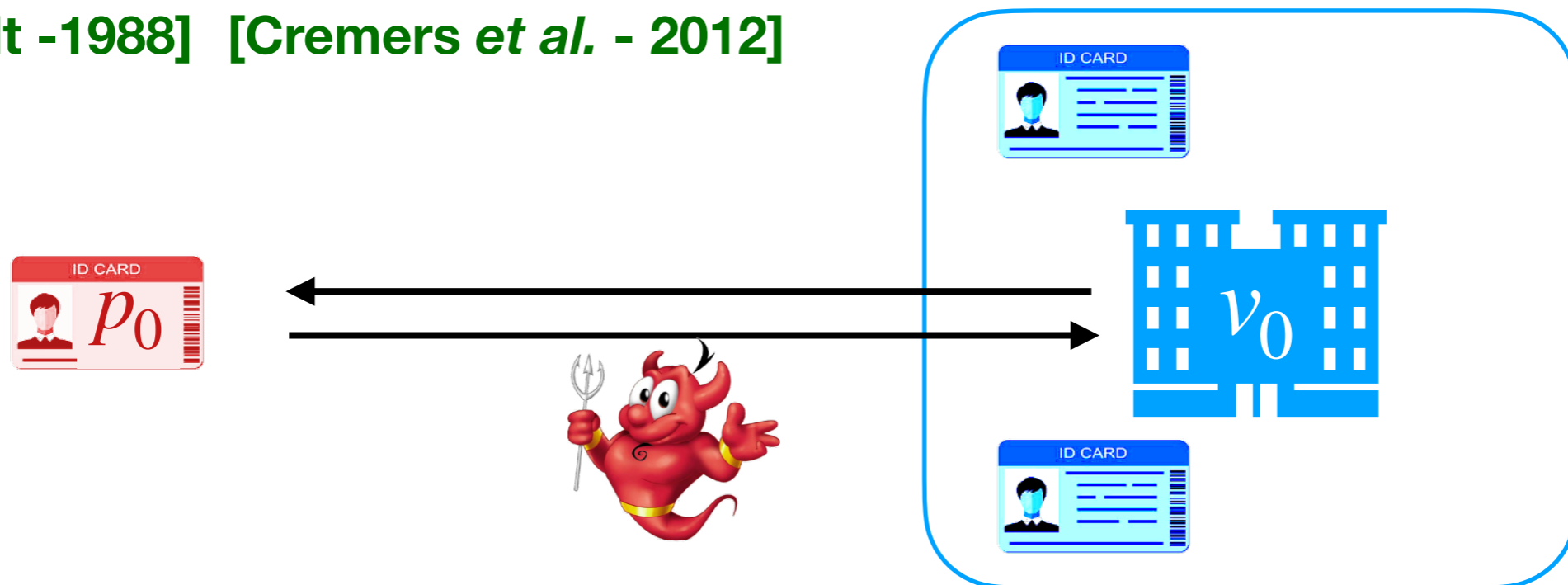
[Desmedt -1988] [Cremers *et al.* - 2012]



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## Definition

A protocol admits a distance hijacking attack if **there exists a topology**

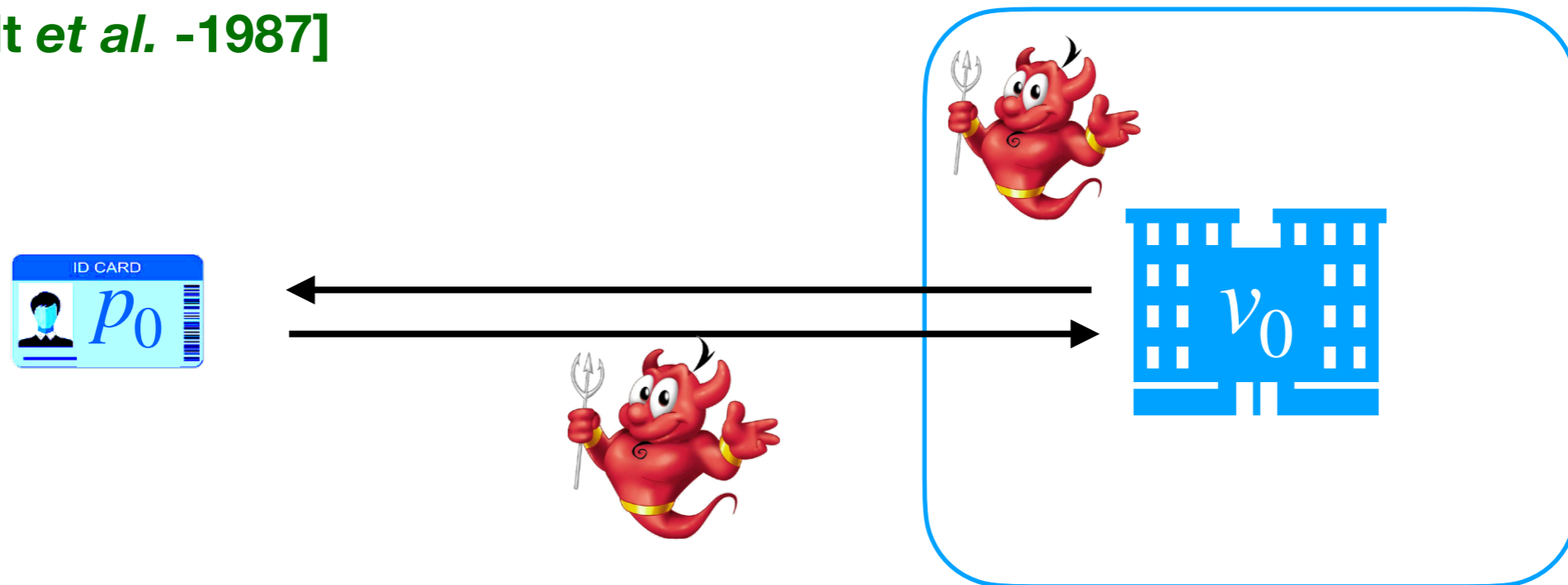
$\mathcal{T} \in \mathcal{C}_{\text{DH}}$  and an initial configuration  $K$  such that:

$$K \longrightarrow (\lfloor \text{end}(v_0, p_0) \rfloor_{v_0}^{t_{v_0}} ; \Phi ; t)$$

# Mafia fraud (MiM attacks)

An **honest verifier** shall not authenticate an **honest and distant prover** even in presence of an **attacker in his vicinity**.

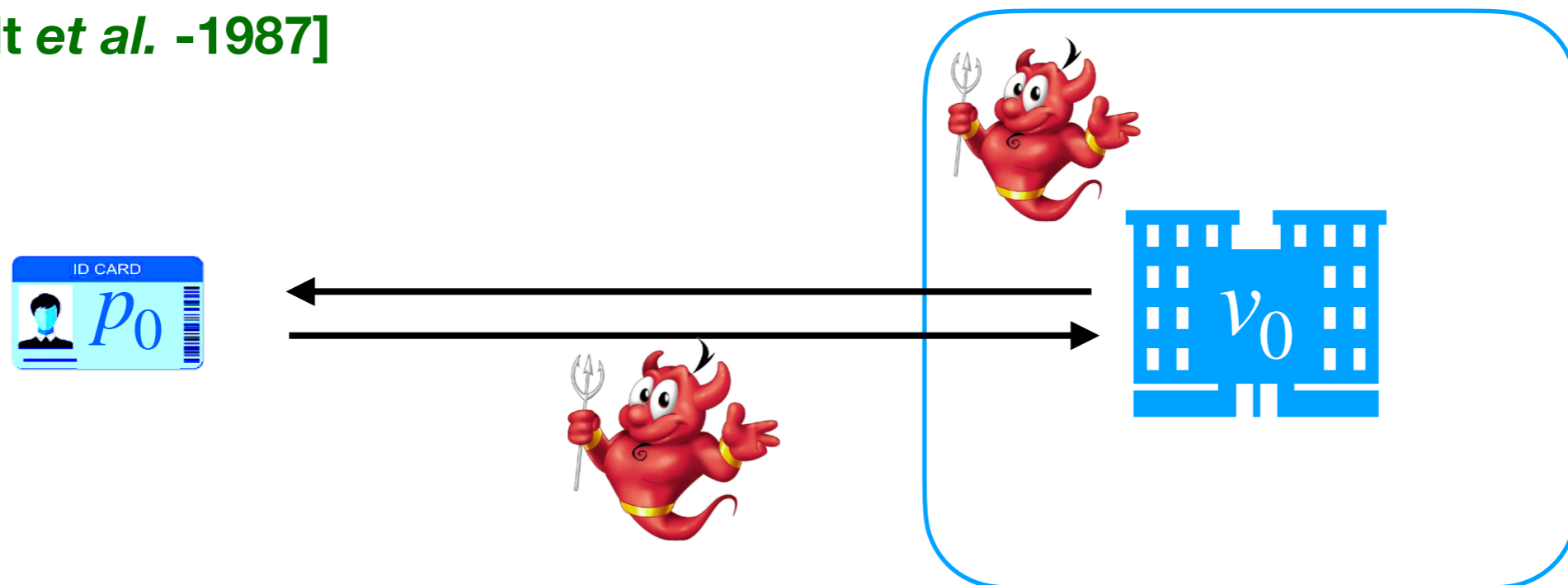
[Desmedt *et al.* -1987]



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## Definition

A protocol admits a mafia fraud if **there exists a topology**  $\mathcal{T} \in \mathcal{C}_{MF}$  and an initial configuration  $K$  such that:

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# **Some reduction results**

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Topologies and time

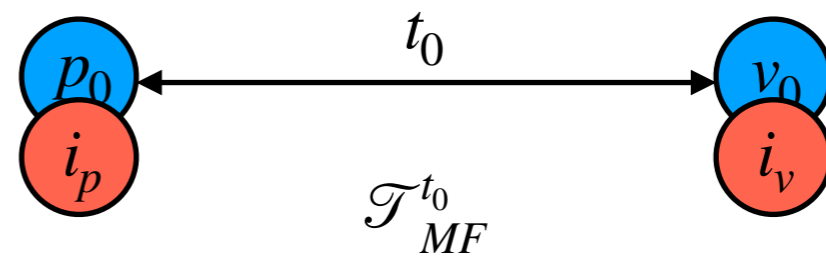
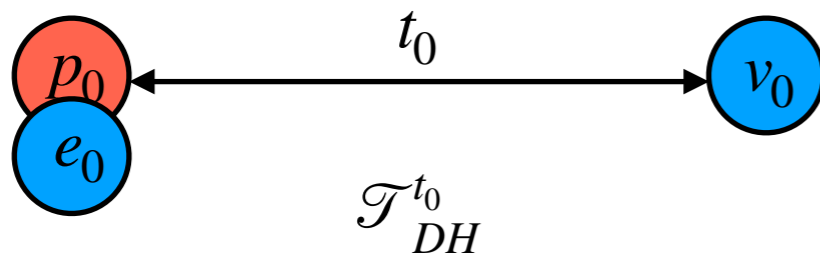
# Main difficulties

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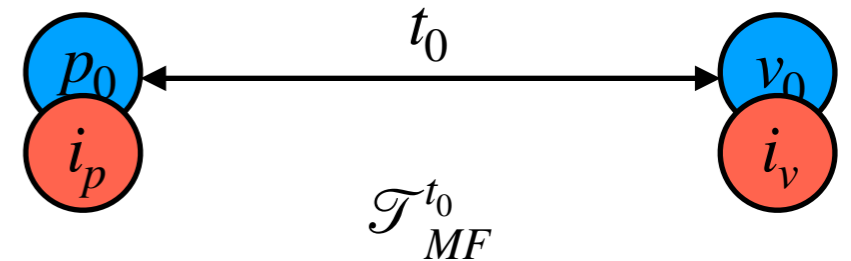
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—> we can use ProVerif's phases to encode the topologies!

# Mafia frauds

## Theorem

A protocol admits a mafia fraud, **if and only if**, there is an attack in  $\mathcal{T}_{MF}^{t_0}$

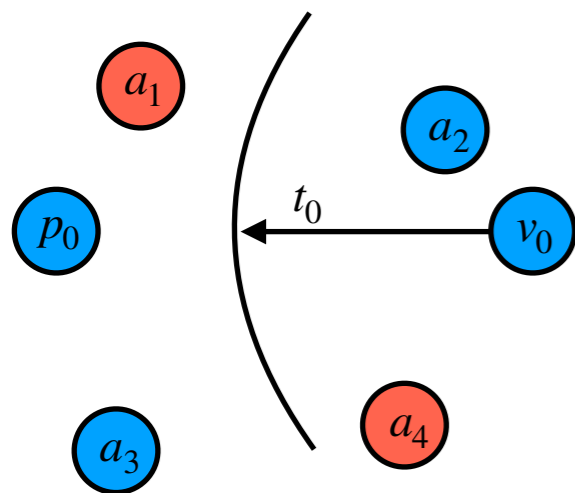


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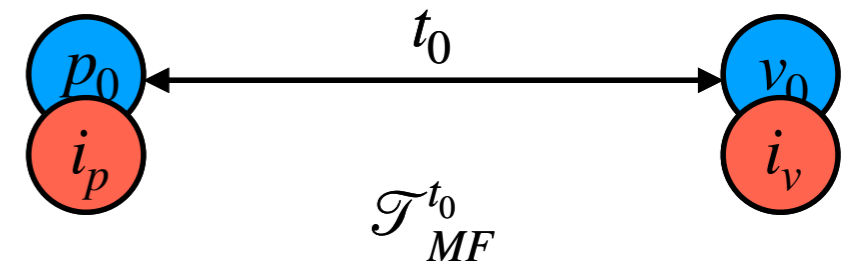
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### Sketch of proof:



An attack trace  
in an **arbitrary**  
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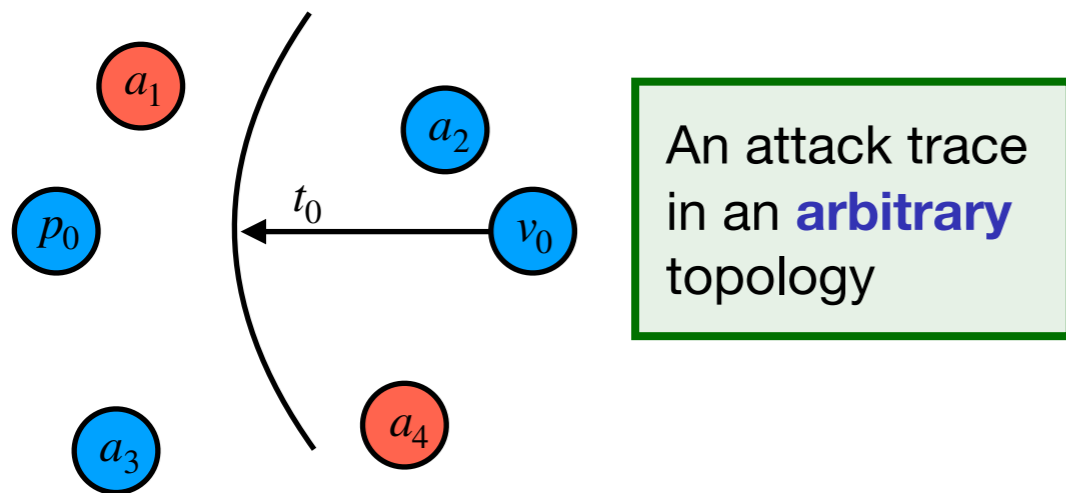


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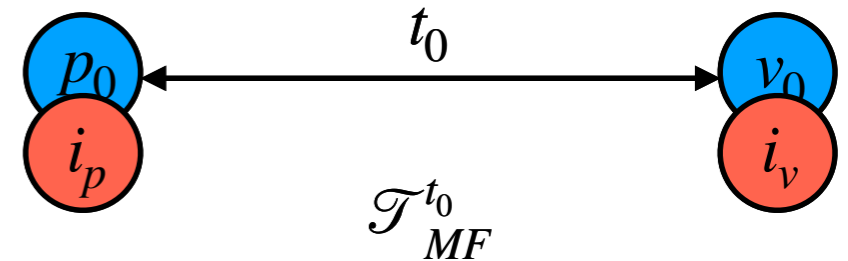
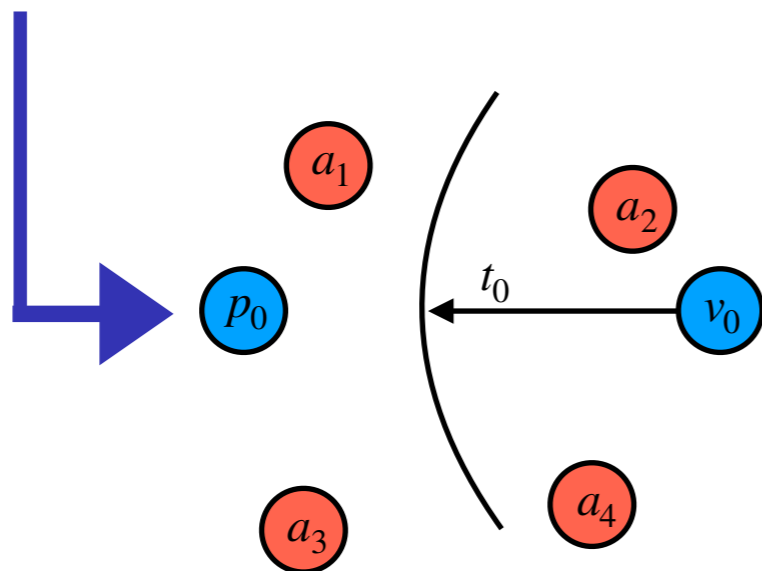
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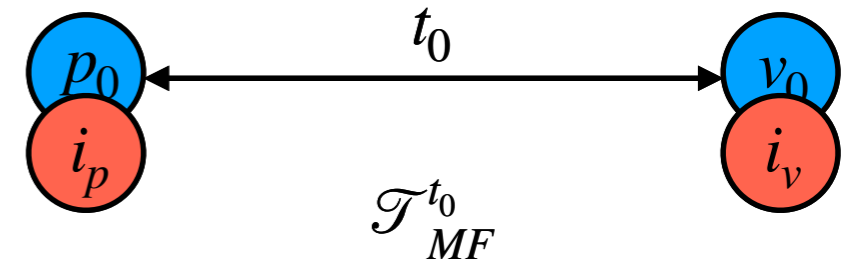
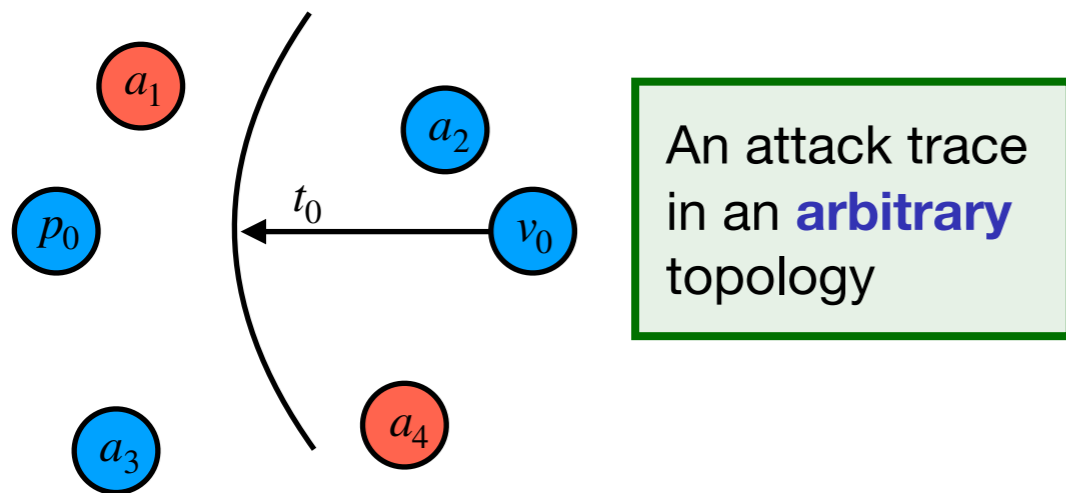


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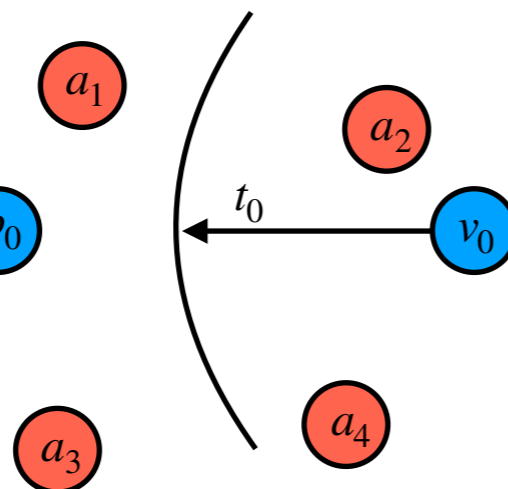
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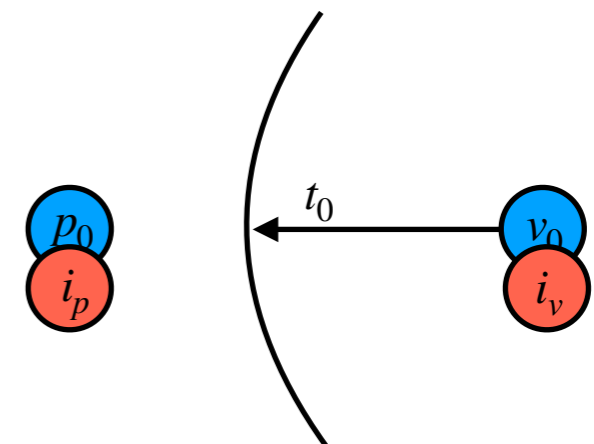


Assume everyone **malicious**



[Nigam *et al.* - 2016]

Place malicious agents **ideally**

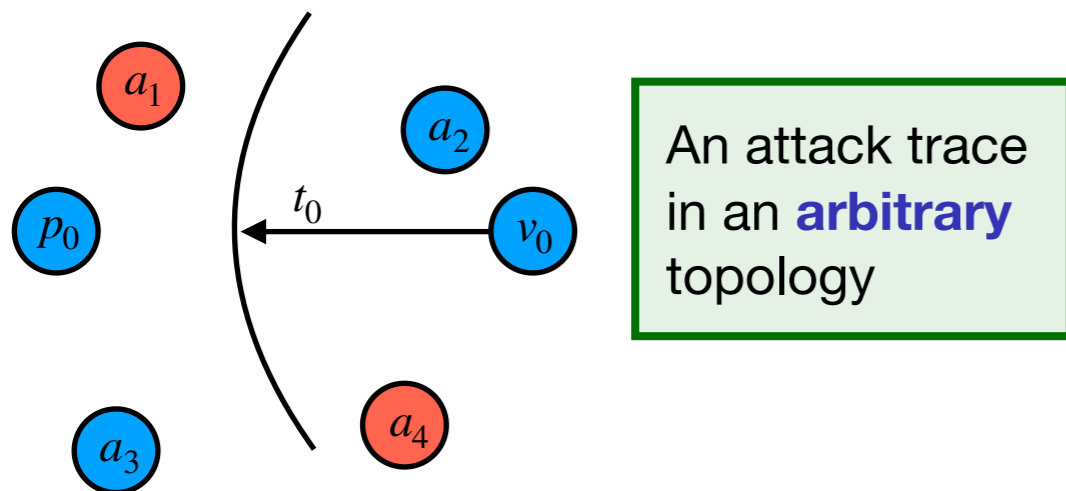


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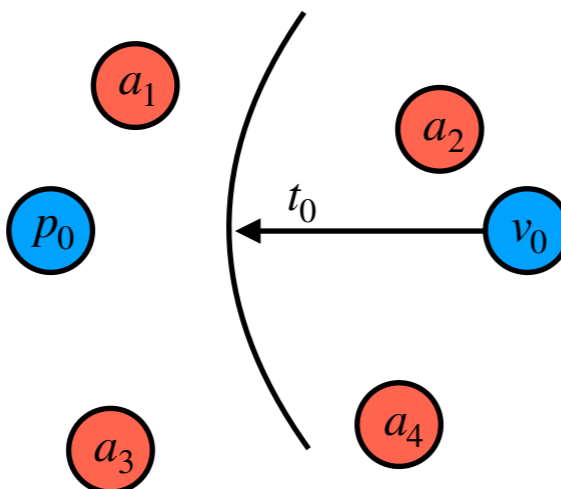
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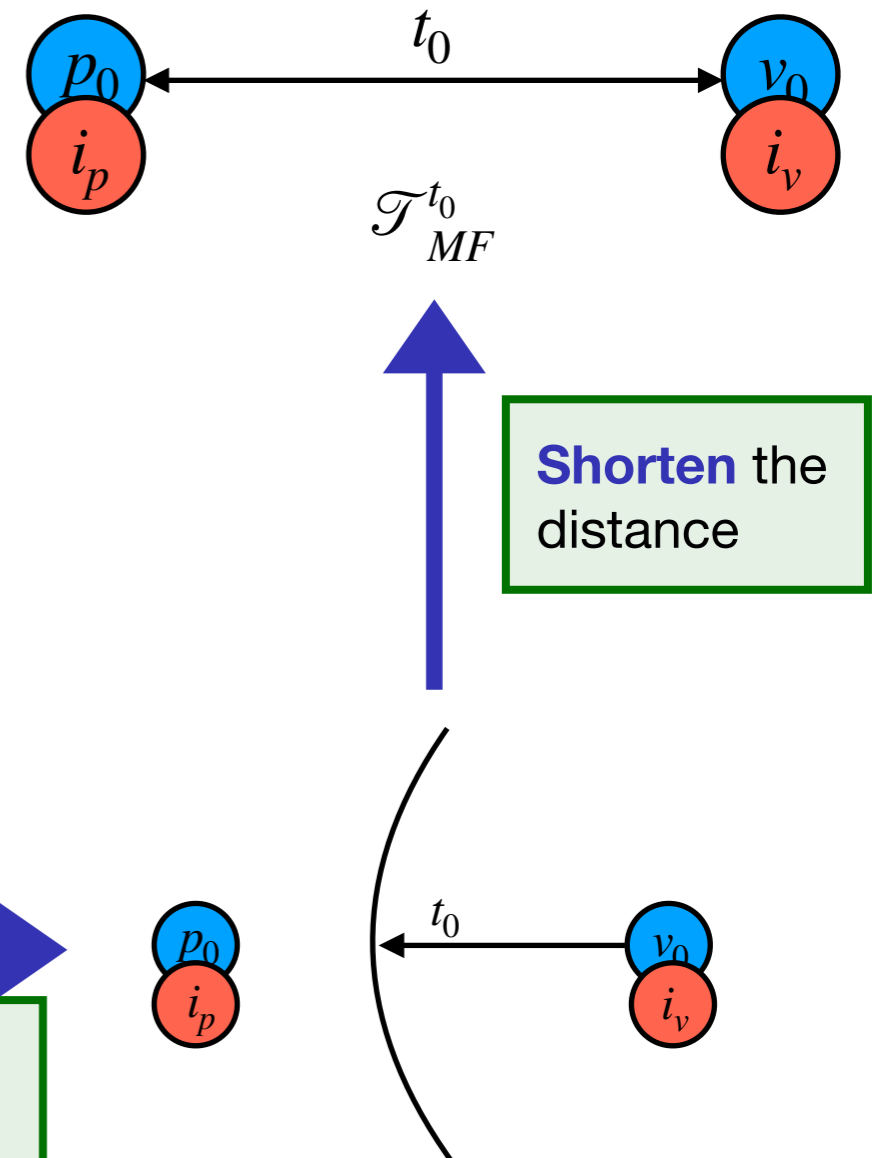


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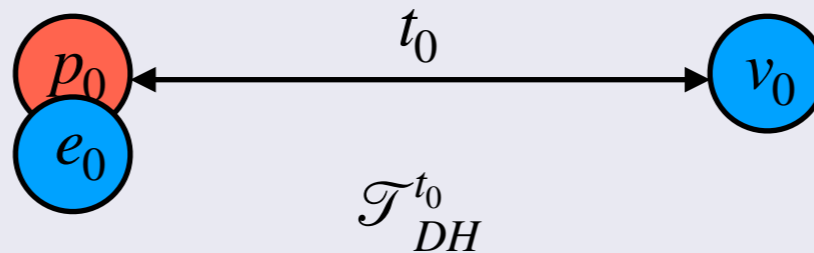
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# Distance hijacking attacks

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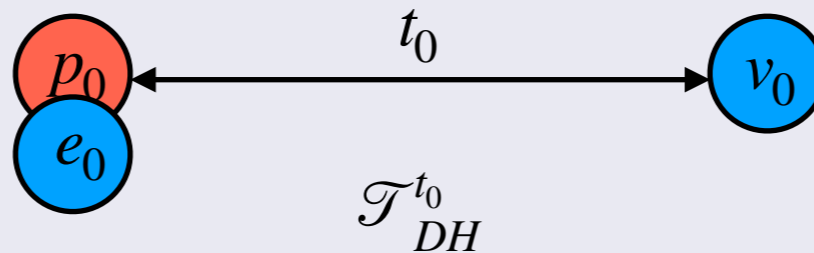
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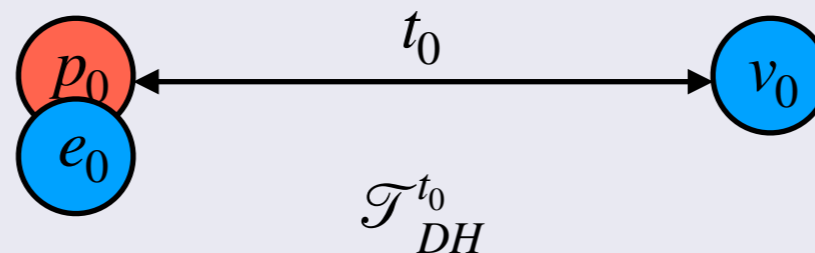
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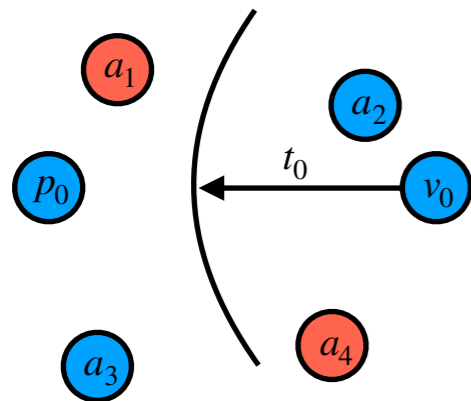
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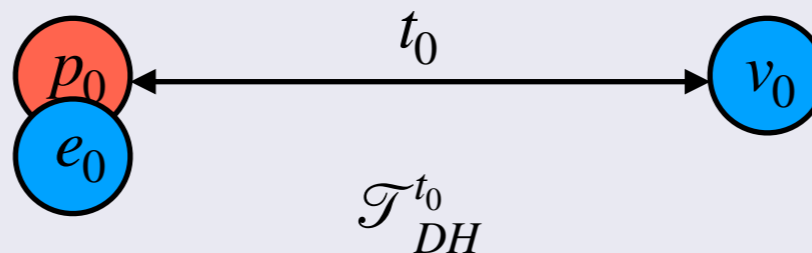


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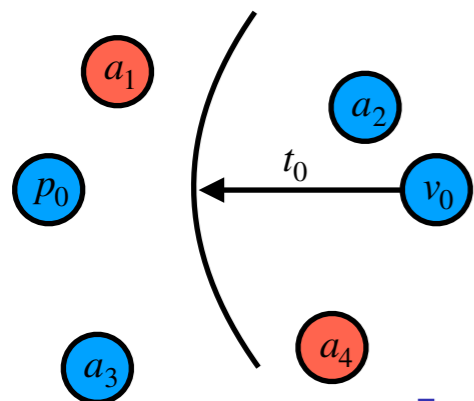
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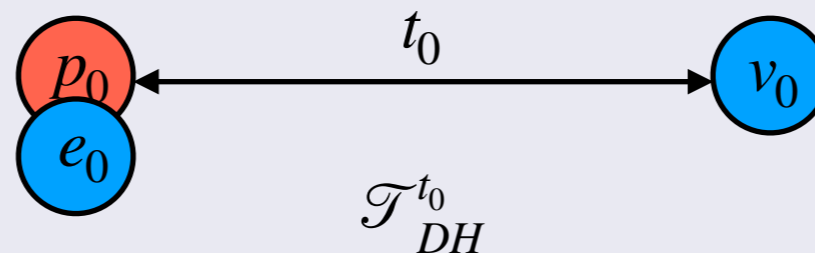
An attack trace  
in an **arbitrary**  
topology

**Untimed** witness of attack

# Distance hijacking attacks

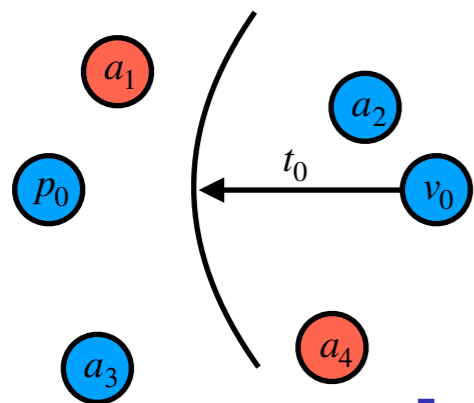
## Theorem

If  $\mathcal{P}_{\text{db}}$  admits a distance hijacking attack, then  $\overline{\mathcal{P}_{\text{db}}}$  admits an attack in  $\mathcal{T}_{DH}^{t_0}$



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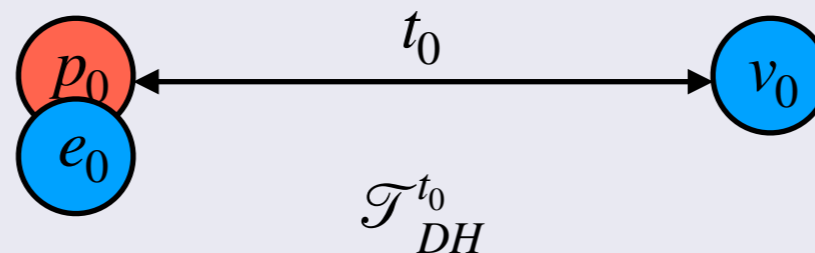
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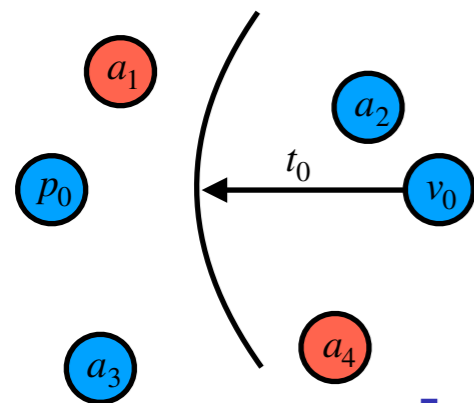
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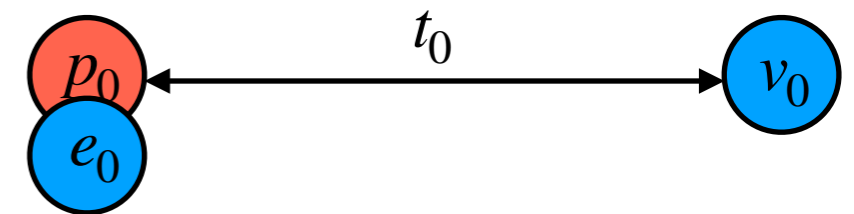
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An attack trace in an **arbitrary** topology

**Untimed** witness of attack

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**Re-timing** the witness

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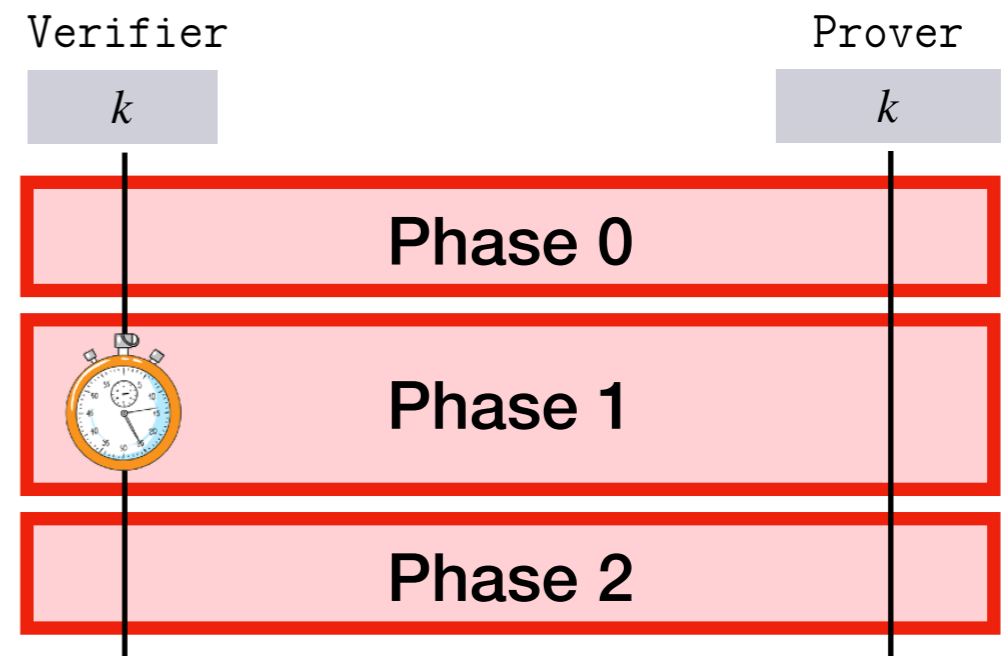
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[Chothia *et al.* - 2015]

➔ it relies on the phases of ProVerif

- ▶ *Phase 0* → *slow initialization phase*
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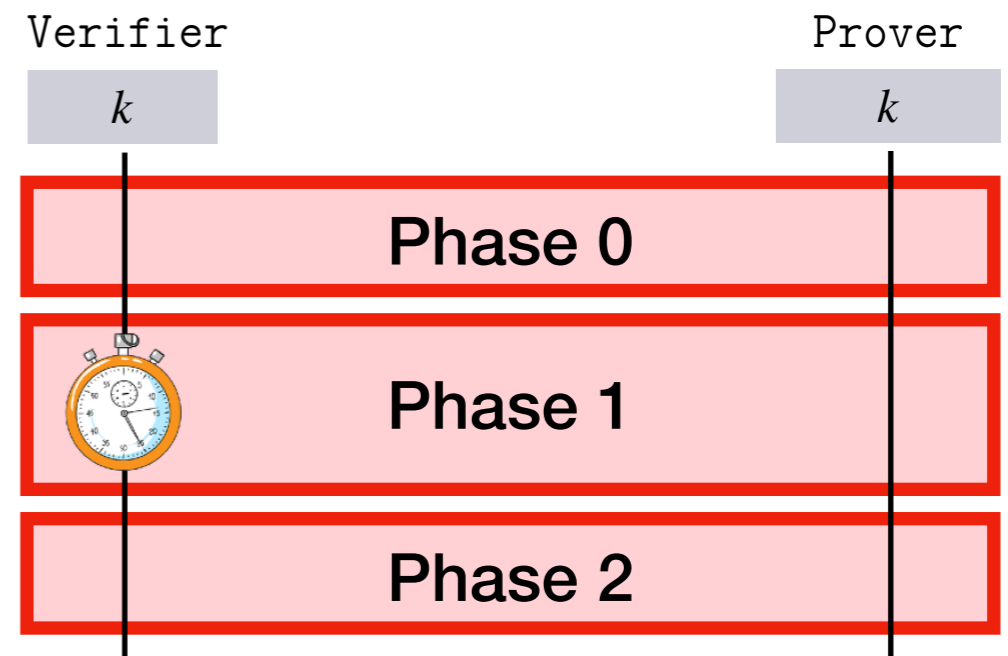
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## Proposition

**If** a protocol  $\mathcal{P}_{db}$  admits a mafia fraud (resp. distance hijacking, terrorist fraud)  
**then**  $\text{end}(v_0, p_0)$  is reachable in  $\mathcal{F}(\mathcal{P}_{db})$ .

# **A comprehensive case studies analysis**

---

Application to  
distance-bounding protocols



# Case studies analyses

**Corpus** +25 protocols

**Tool** ProVerif (slightly modified for distance hijacking attacks)

- Abstractions**
- ▶ rapid phase collapsed in a single round-trip
  - ▶ weak exclusive-OR

tool limitation

model limitation

## Application to real-world protocols

Protocols	Mafia fraud	Distance hijacking	Terrorist fraud
MasterCard RRP	✓	✗	✗
PaySafe	✓	✗	✗
MIFARE Plus	✓	✗	✗

# Conclusion

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# Finally we have...

Symbolic model

1. **Syntax and semantics** for describing protocols
2. Formally define the **security properties**

New tools

Reduction results to leverage existing tools

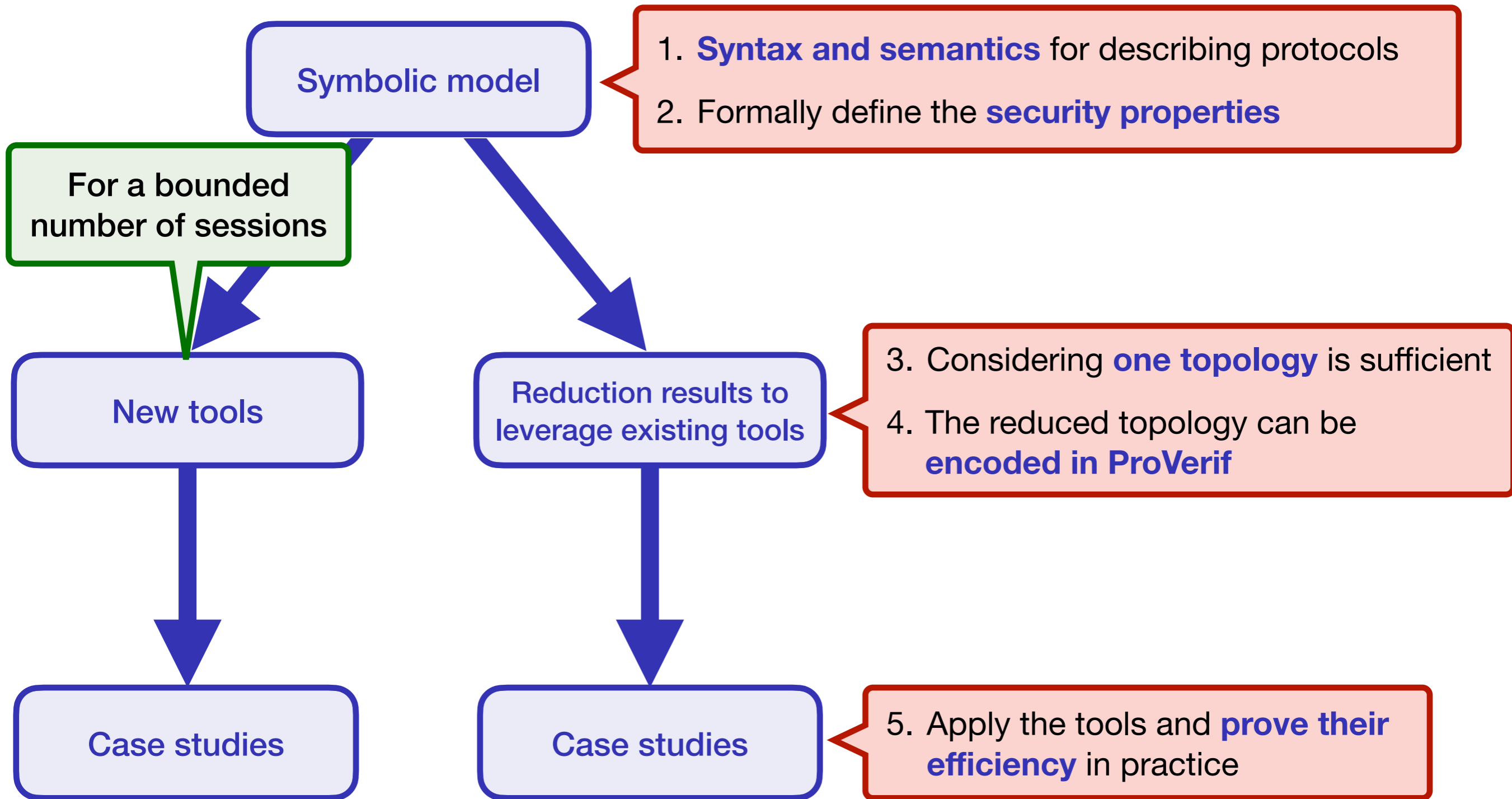
3. Considering **one topology** is sufficient
4. The reduced topology can be **encoded in ProVerif**

Case studies

Case studies

5. Apply the tools and **prove their efficiency** in practice

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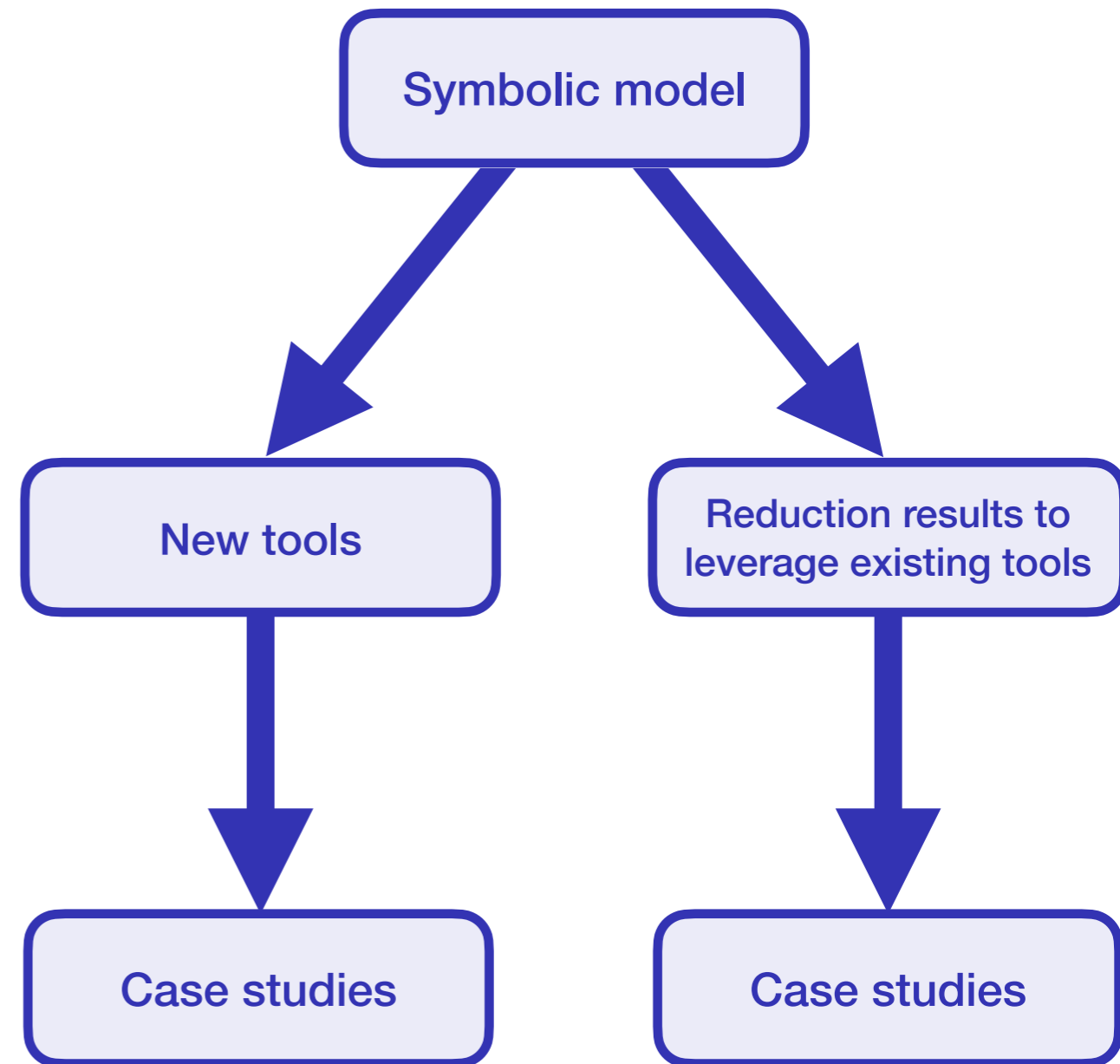


# Future work

Remove hypotheses in the theorems

Make the existing tools support exclusive-OR

- ▶ extend ProVerif's procedure
- ▶ improve automation for Tamarin



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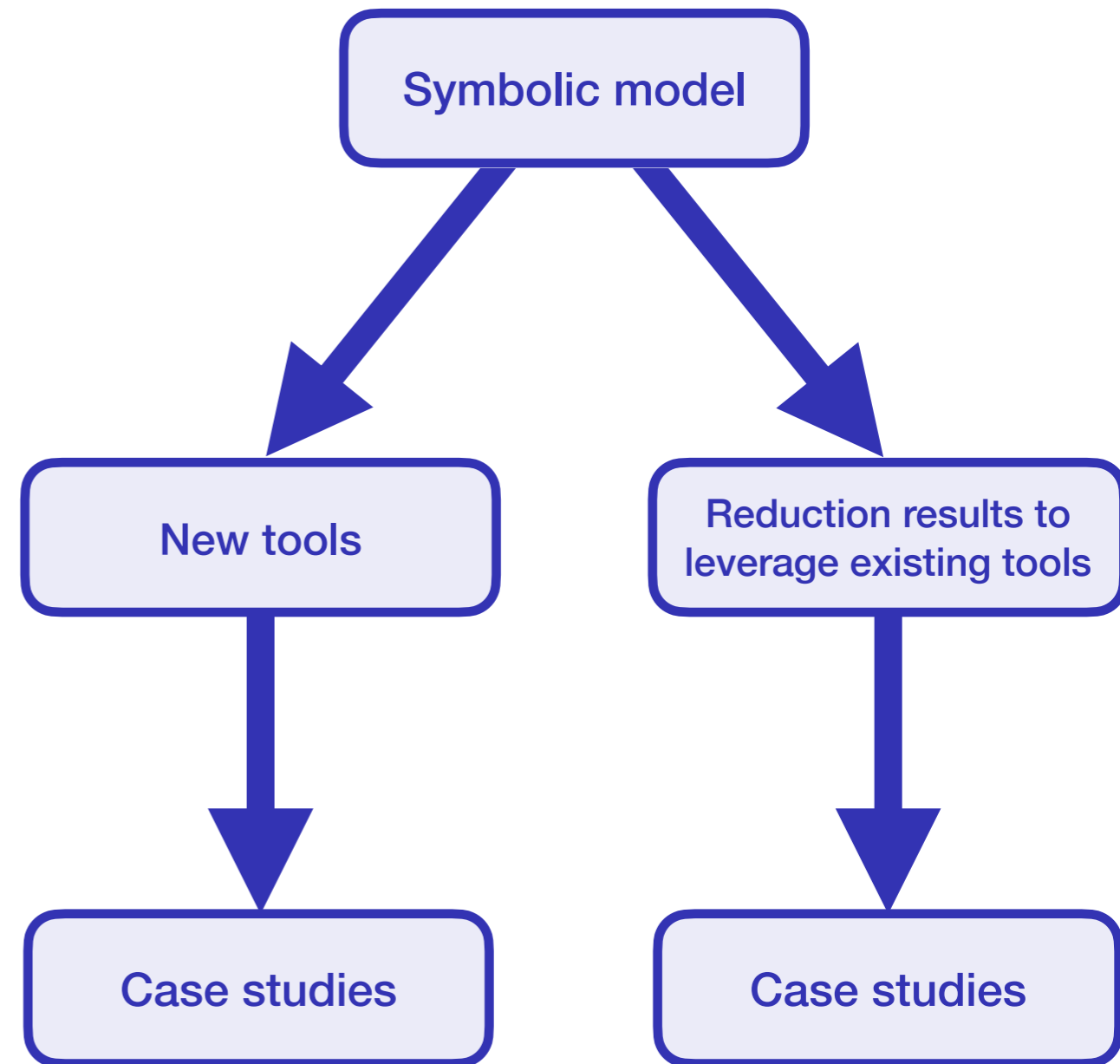
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**Improve the model of time**

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**Model bit-level operations**

- ▶ consider probabilistic processes and properties
- ▶ model messages with bitstrings

