

Deciding equivalence properties in security protocols

Vincent Cheval, Steve Kremer, [Itsaka Rakotonirina](#)

INRIA Nancy Grand-Est, LORIA

Security protocols

Google SSO

BAC (e-passport)

Helios (e-voting)

TLS 1.3 (prior ver.)

WPA2 (wifi)

Security protocols

Google SSO

 Armando *et al.* (2008)

BAC (e-passport)

 Chothia and Smirnov (2010)

Helios (e-voting)

 Cortier and Smyth (2011)

TLS 1.3 (prior ver.)

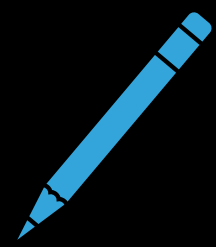
 Cremers *et al.* (2016)

WPA2 (wifi)

 Vanhoef and Piessens (2017)

Security protocols

The attacker can...



Read / Write



Intercept

But they do not...



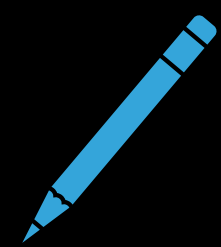
Break cryptography



Use side channels

Security protocols

The attacker can...



Read / Write



Intercept

But they do not...



Break cryptography



Use side channels

Dolev-Yao models

Concurrent systems where dishonest parties have complete control over inter-process communication

but cryptography is idealised

Security properties

Reachability

Bad event in one system



Authentication



(weak) secrecy

Equivalence

Privacy as indistinguishability



Anonymity



Vote privacy



Unlinkability

Security properties

Reachability ✓

Bad event in one system



Authentication



(weak) secrecy

Equivalence ?

Privacy as indistinguishability



Anonymity



Vote privacy



Unlinkability

Tool support

Equivalence

Privacy as indistinguishability

Tamarin

Maude-NPA

ProVerif

Akiss

SAT-equiv

SPEC

Tool support

Equivalence

Privacy as indistinguishability

may not terminate

bounded number of
protocol sessions

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approximation of equivalence
(false attacks)

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approximation of equivalence
(false attacks)

crypto limited to a few
(common) primitives

Contributions

DEEPSEC prover

may not terminate

approximation of equivalence
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crypto limited to a few
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bounded number of
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Contributions

DEEPSEC prover

~~may not terminate~~

~~approximation of equivalence
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bounded number of
protocol sessions

exact procedure
for trace equivalence

any subterm convergent
constructors/destructors

Contributions

DEEPSEC prover

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~~approximation of equivalence
(false attacks)~~

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exact procedure
for trace equivalence

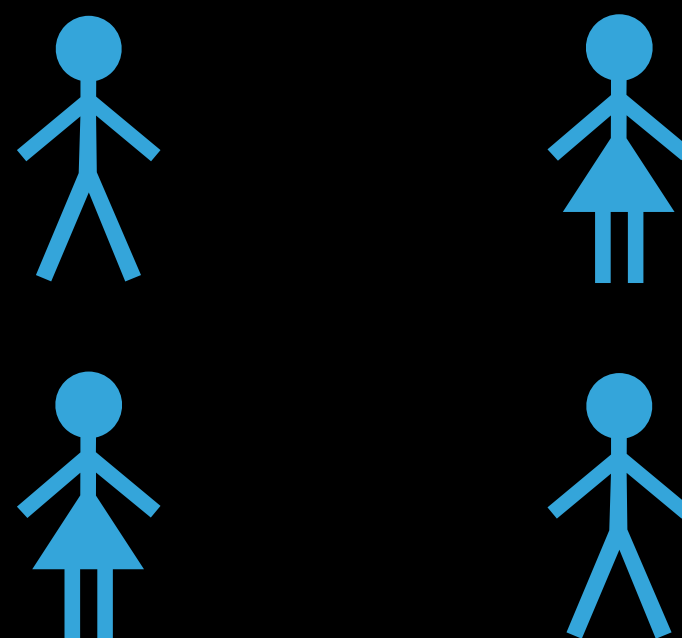
any subterm convergent
constructors/destructors

+ running implementation

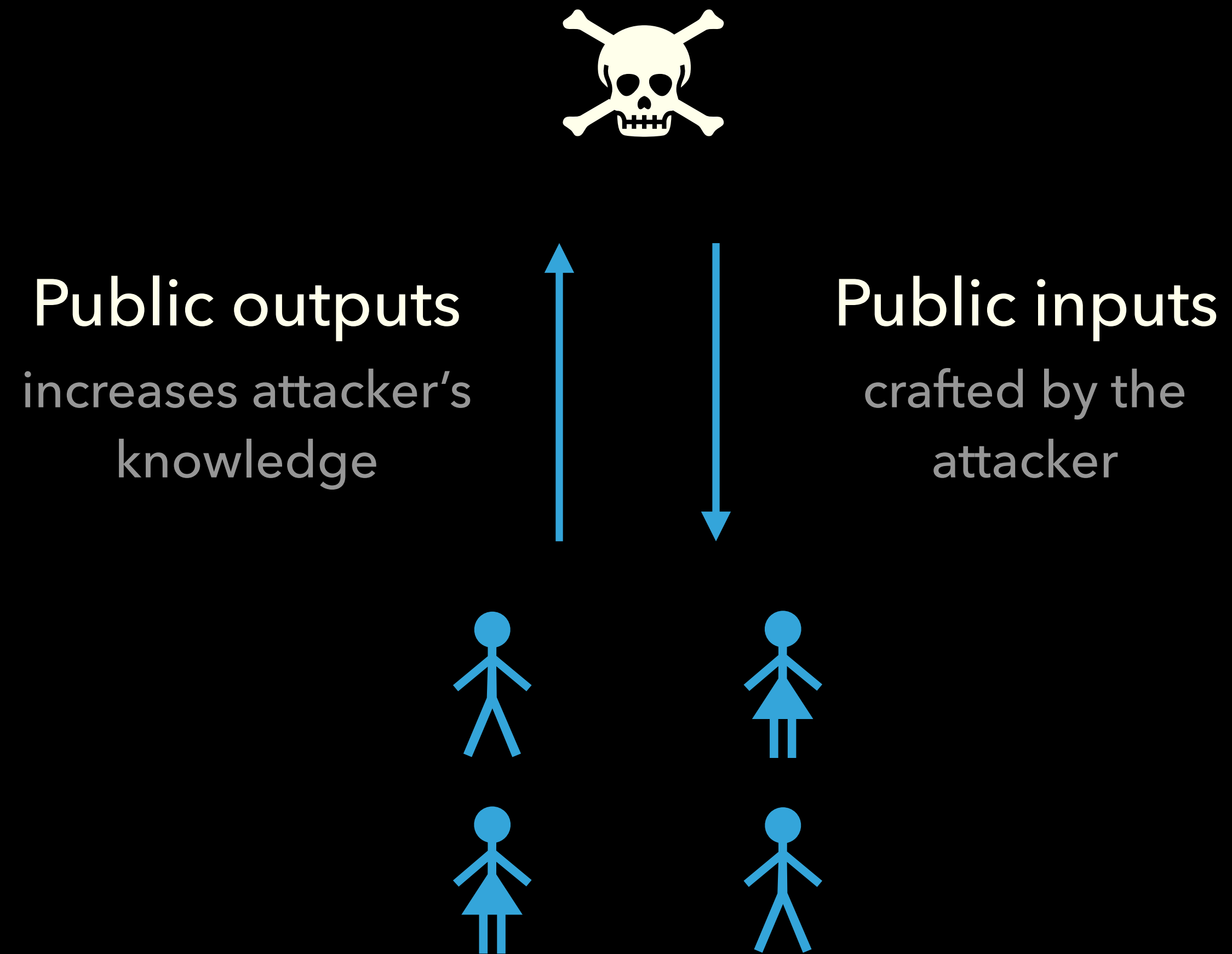
+ tight complexity analysis of the problem

ANALYSING FINITE PROCESSES

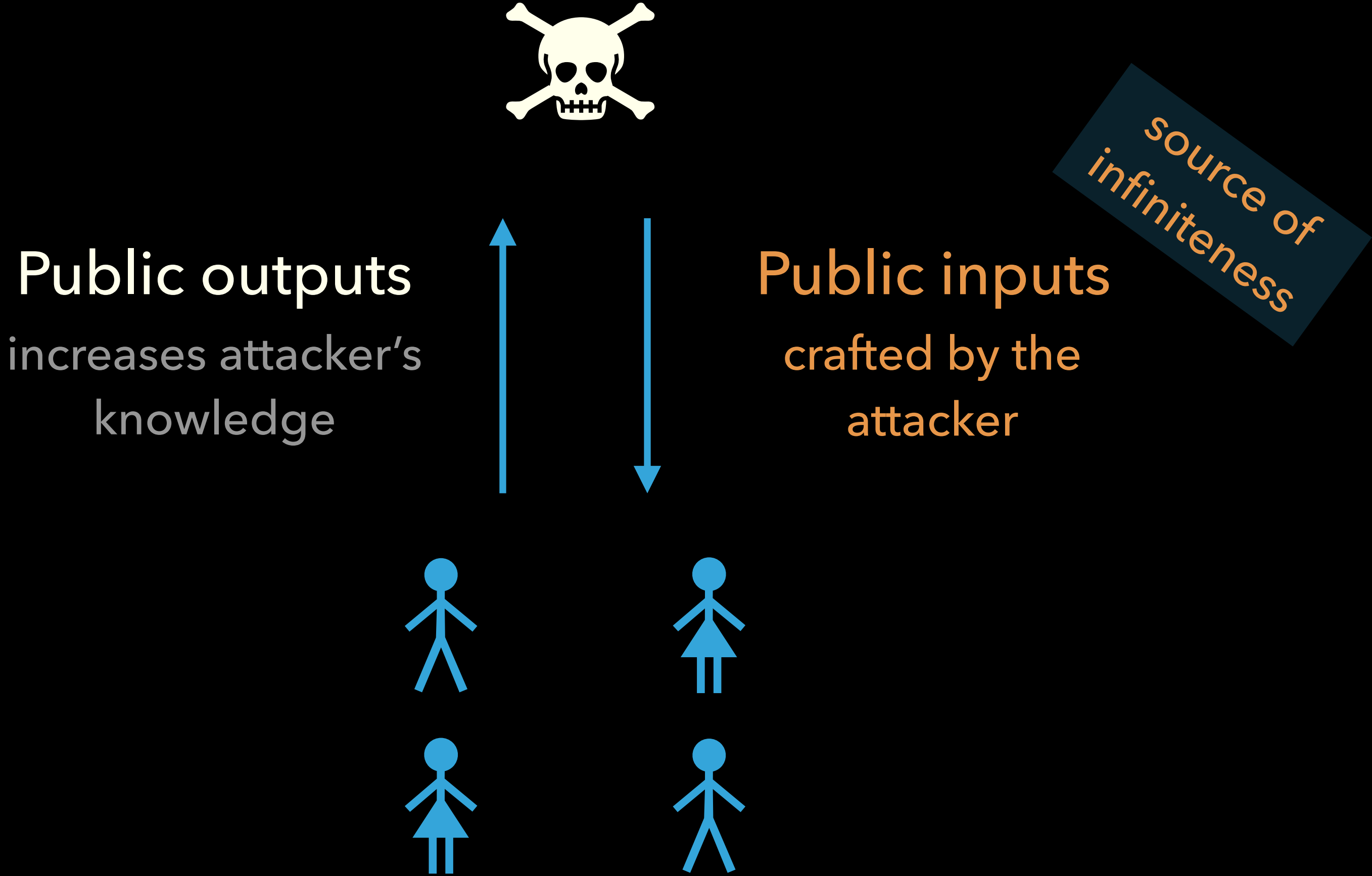
The problem



The problem



The problem



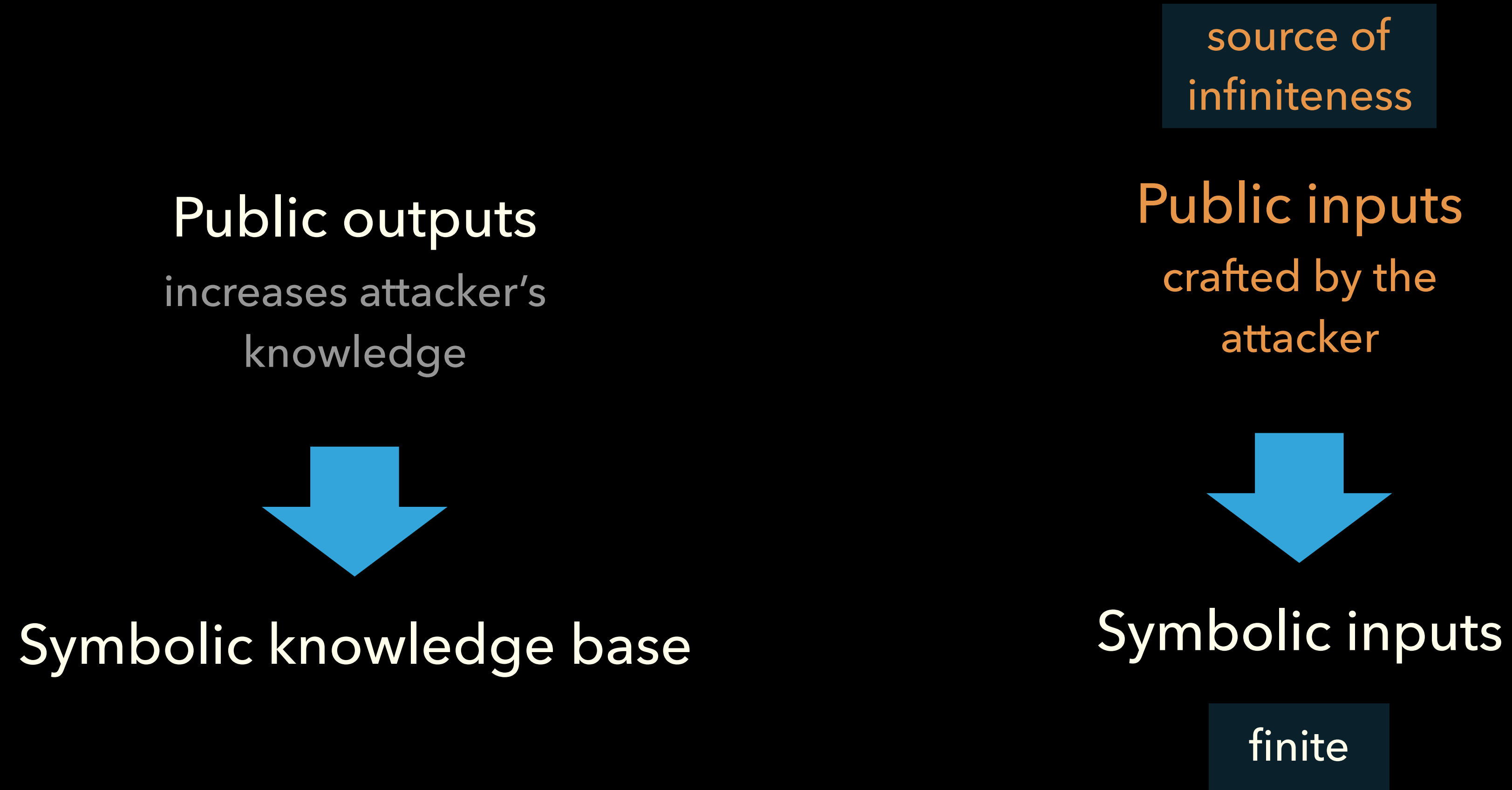
The problem

source of
infiniteness

Public outputs
increases attacker's
knowledge

Public inputs
crafted by the
attacker

The problem



Handling the symbolic setting

Symbolic knowledge base

+

Symbolic inputs

Handling the symbolic setting

Symbolic knowledge base

+

Symbolic inputs

Symbolic constraints
to characterize symbolic traces

Handling the symbolic setting

Symbolic knowledge base

+

Symbolic inputs

Symbolic constraints

to characterize symbolic traces

$$X \vdash^? x$$

Deducibility constraints

ability for the attacker to craft x
(modulo crypto primitives)

$$x \stackrel{?}{=} y$$

Equations

equality of two terms

Decidability

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Equations

equality of two terms

Ingredients

Most general solutions

of a symbolic trace

+

Tree of sets of symbolic traces

built by constraint solving
equivalence = reachability of a **BAD** node

Comparison to other tools

	#Agents	AKISS	SATEQUIV	DEEPSEC
Wide-Mouth Frog (strong secrecy)	6 ✓	<1s	<1s	<1s
	12 ✓	22min	<1s	<1s
	23 ✓	OOM	<1s	3s
Helios Vanilla (vote privacy)	6 ⚡	47s	—	<1s
Helios Weeding	6 ✓	OOM	—	1s
Helios Zero-KP	6 ✓	OOM	—	2s
Helios W revote	11 ⚡	OOM	—	2s
Helios ZKP revote	11 ✓	OOM	—	2h 42min

✓ security proof

⚡ security violation

— cannot be specified

OOM out of memory

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COULDN'T IT BE MORE EFFICIENT?

For subterm convergent crypto



Passive attacker

PTIME

with fixed cryptographic
primitives



Active attacker

coNP-complete

if no **else** branches +
each honest agent uses a different channel

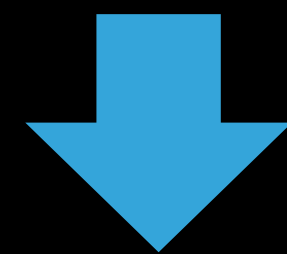
For subterm convergent crypto



Passive attacker

PTIME

with fixed cryptographic
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coNP-complete

in general

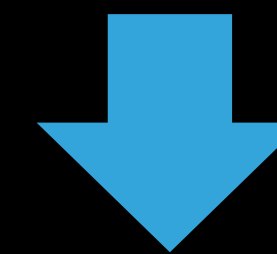
new!



Active attacker

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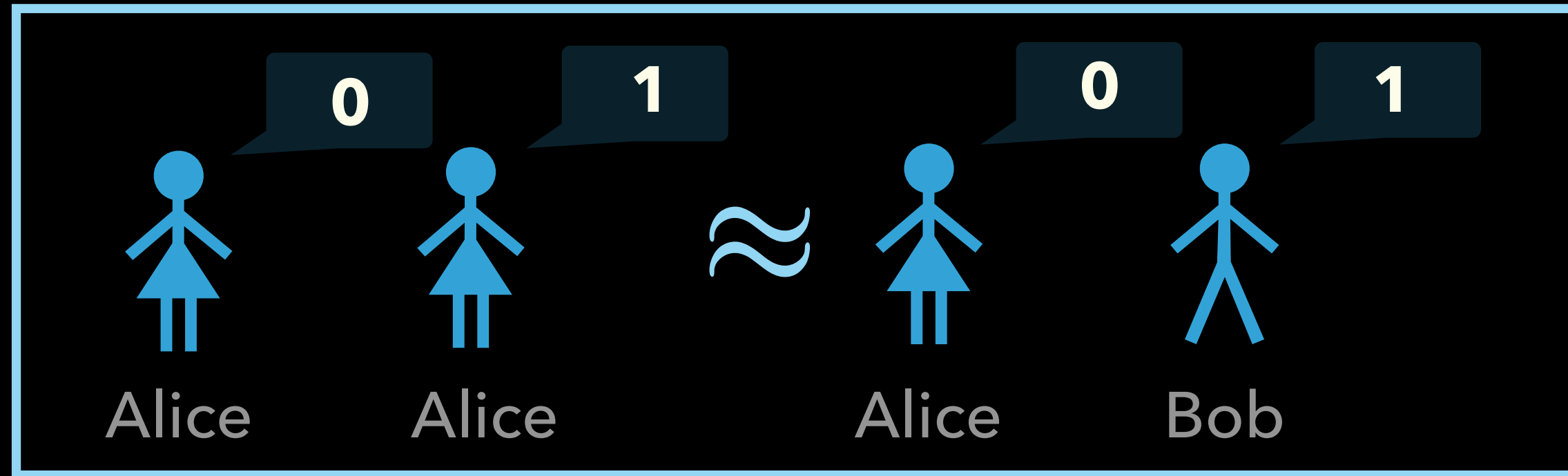


coNEXP-complete

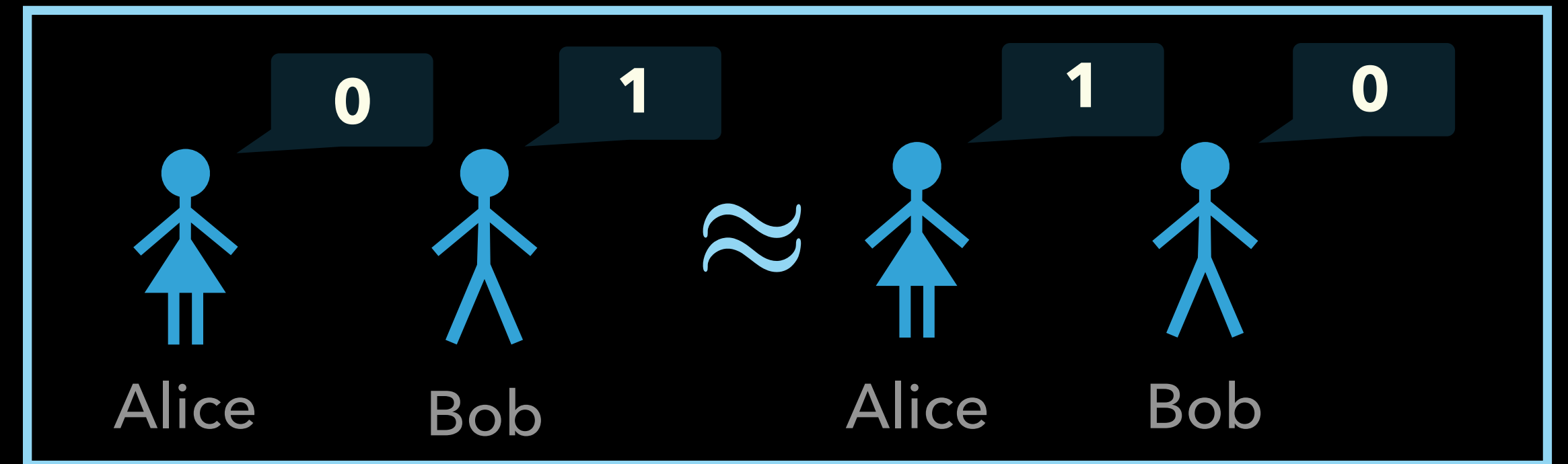
in general

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But in practice?

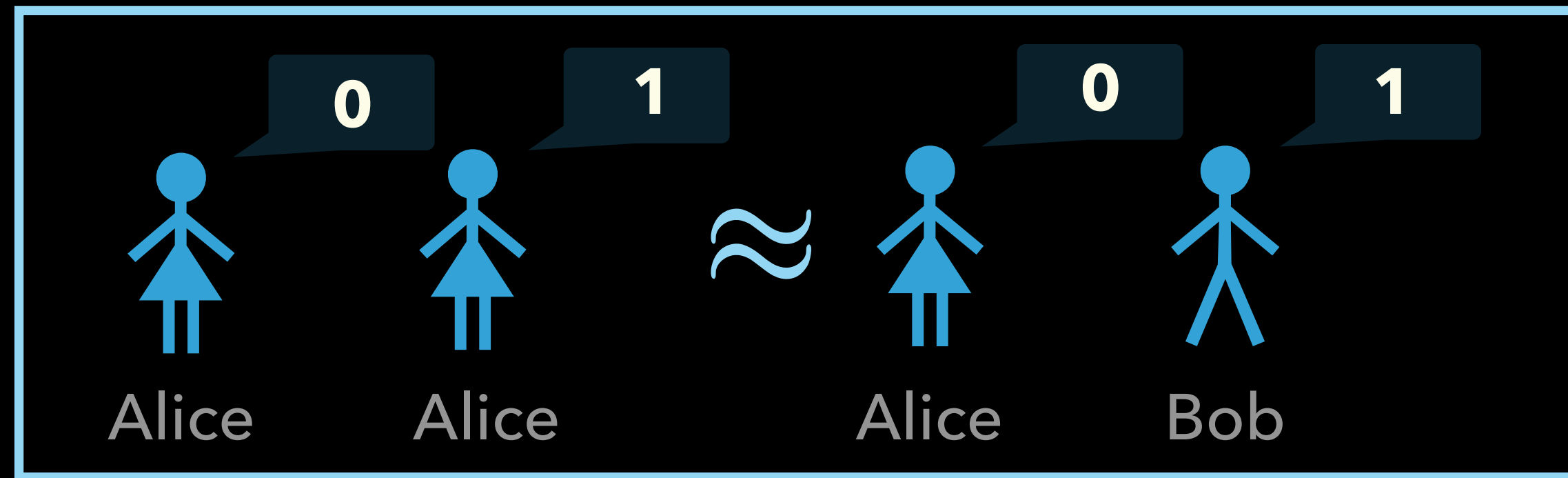


Unlinkability

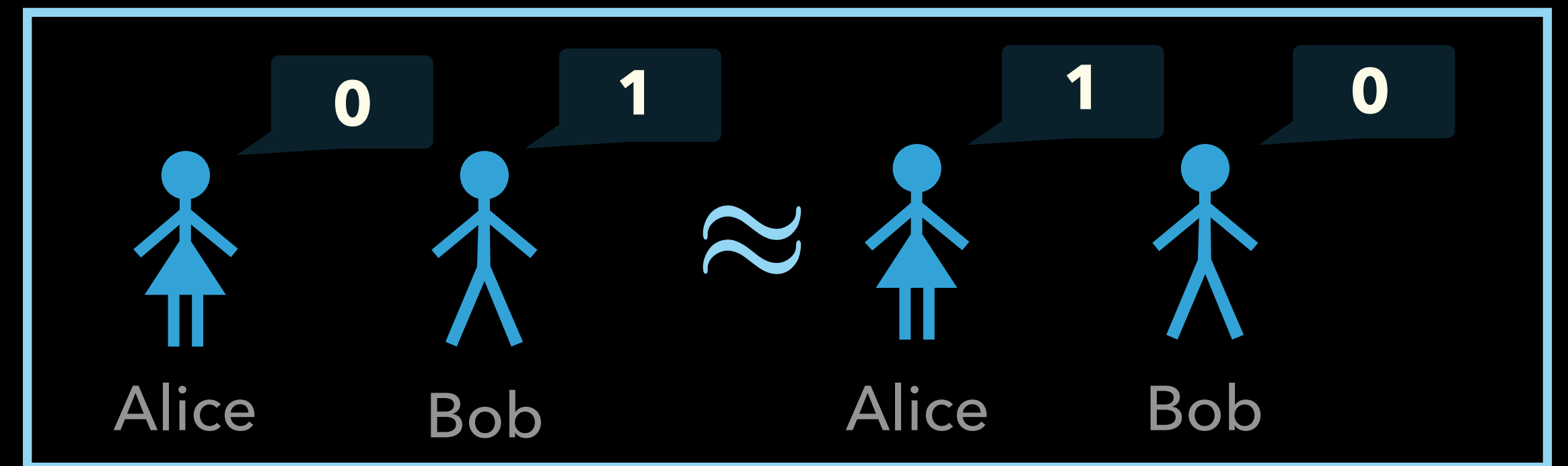


Vote privacy

But in practice?



Unlinkability

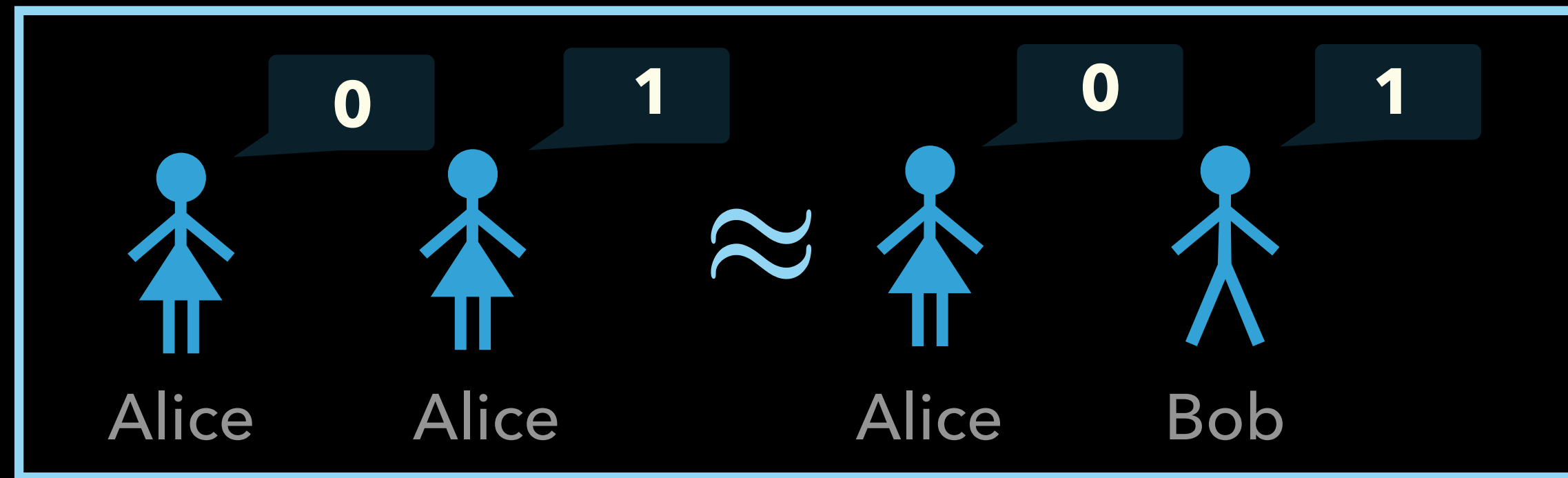


Vote privacy

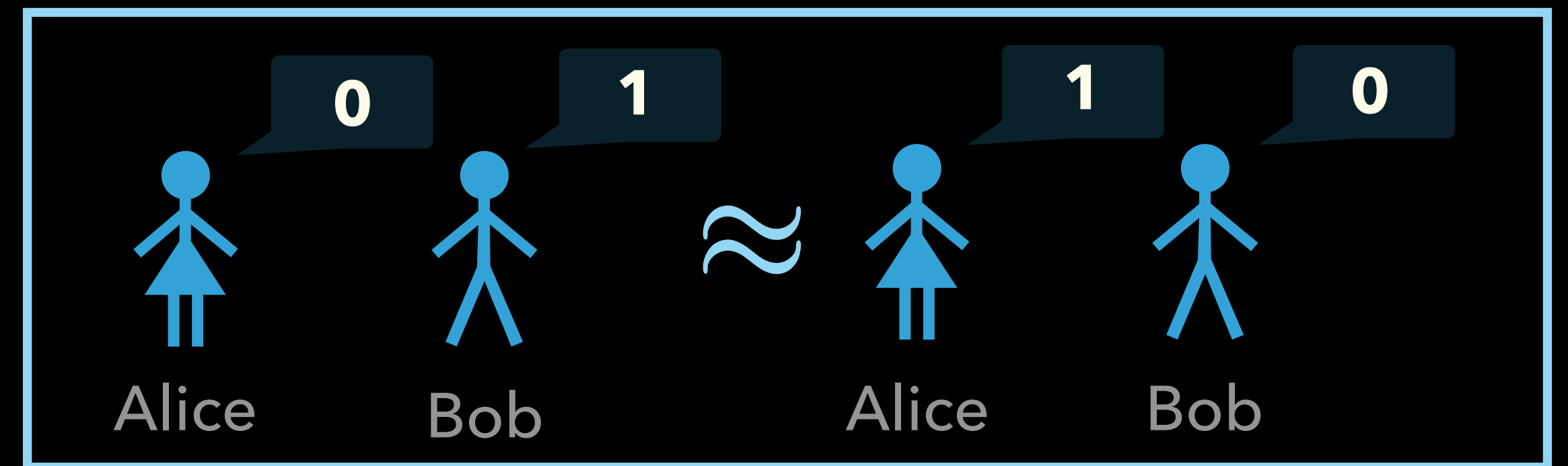
Observation

In practice, we check equivalence of processes with similar structure

But in practice?



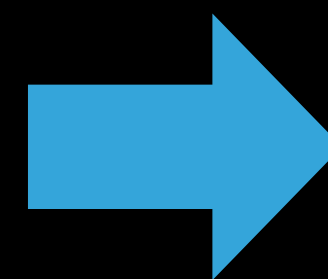
Unlinkability



Vote privacy

Observation

In practice, we check equivalence of processes with similar structure



Future work

Speed-up of the procedure in practical cases by using symmetry reductions

CONCLUSION

Conclusion



logical flaws of
security protocols

Conclusion

Exact Analysis
without approximations
+ full finite fragment



logical flaws of
security protocols

Conclusion




Conclusion

Implementation

available at

<https://deepsec-prover.github.io>



logical flaws of
security protocols

Exact Analysis

without approximations
+ full finite fragment

"Optimal" Complexity

coNEXP-hardness
of the problem