Improving Automated Symbolic Analysis of Ballot Secrecy for E-voting Protocols:
A Method Based on Sufficient Conditions

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Extremely complex setting

- insecure network
- active attacker
- parties running concurrently

Formal methods

- mathematical \& exhaustive analysis
- formal guarantees
- automated \& mechanised


## Symbolic Model

Cryptographic primitives assumed perfect

- primitives modelled as function symbols \& equational theory
- e.g. $\because, \bigodot$ en $(\cdot, \cdot), \operatorname{dec}(\cdot, \cdot) \& \operatorname{dec}(\operatorname{enc}(m, k), k)=m$

Security protocols

- each party $\longmapsto$ process in a process algebra

Attacker = network (worst case scenario)

- eavesdrop: he learns all protocol outputs
- injections: he chooses all protocol inputs


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Security properties encoded as:

- reachability statements (e.g. for secrecy)
- or behavioral equivalence statements (e.g. for privacy)

Benefit: high level of automation and tool support!

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- or behavioral equivalence statements (e.g. for privacy)

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## Symbolic Verification of E-Voting Protocols

Remote E-Voting Protocols:

- actually used: Estonia, Australia, Switzerland, many smaller elections
- 2 crucial properties: verifiability (of the election) and privacy (of the votes)
- hard to get right + extremely strong threat model


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- hard to get right + extremely strong threat model

This Work: Improve ballot privacy verification technique

- new verification technique based on sufficient conditions
- extends the scope + more efficient


## Introduction

| State-of-the-Art \& Limitations
II Our Approach: Sufficient Conditions for Privacy
III Conclusion

## Applied $\pi$-Calculus

Model of messages: function symbols \& equational theory
Model of protocols: Process algebra

- Process:

$$
\begin{aligned}
P, Q & := \\
& \operatorname{in}(c, x) \cdot P \\
& \mid \\
& \operatorname{out}(c, m) \cdot P \\
& i: P
\end{aligned}
$$

input
output
phase (can be executed >= phase i)

## Applied $\pi$-Calculus

Model of messages: function symbols \& equational theory
Model of protocols: Process algebra

- Process:

input
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phase (can be executed >= phase i)
parallel
replication
conditional
creation of name
null


## Applied $\pi$-Calculus

Model of messages: function symbols \& equational theory
Model of protocols: Process algebra

- Process:

| $P, Q$ | $:=\operatorname{in}(c, x) \cdot P$ | input |
| ---: | :--- | ---: |
|  | $\|$$\operatorname{out}(c, m) \cdot P$ output <br> $i: P$ phase (can be executed $>=$ phase i) <br>  $P \mid Q$ <br> $\mid P$ parallel <br>  if Test then $P$ else $Q$ | replication |
|  | new $X \cdot P$ | conditional |
|  | 0 | creation of name |
|  |  | null |

- Frame $(\phi)$ : the set of messages revealed to
(*) sknowledge)
- Configuration: $A=(\mathcal{P} ; \phi ; j)$
( $\mathcal{P}$ multiset of processes, $j \in \mathbb{N}$ )


## E-Voting and Privacy

## E-Voting Protocol (simplified)

- Roles as processes: Voter: $V(\mathbb{Q})$ and authorities: $A \in \mathcal{R}$
- Tally as a function Tally over frames
- Honest Trace: a fixed, full, honest execution of $\{V(\sqrt{6}, \checkmark)\} \cup \mathcal{R}$


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Where $\approx$ is a behavioral equivalence:
cannot establish meaningful link between a voter and his vote"

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Ballot Privacy (simplified)

Where $\approx$ is a behavioral equivalence:

## cannot tell both sides apart.

Trivial Example:

$$
V(\sqrt{9}):=1: \operatorname{out}(c, 9) \cdot \operatorname{out}(c, \text {, })
$$

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## Ballot Privacy (simplified)

Where $\approx$ is a behavioral equivalence: cannot tell both sides apart.

$\sim$ has to let both and reach phase 2 before getting any

## Problem

State-of-the-art: $\approx$ approximated by "diff-equivalence" (when $\infty$ sessions) Ballot privacy: $V(\stackrel{A}{(1)}, \sqrt{ })|V(\times)|!\mathcal{A} \approx V(\times)|V(\sqrt{\infty})|!\mathcal{A}$

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State-of-the-art: $\approx$ approximated by "diff-equivalence" (when $\infty$ sessions) Ballot privacy: $V(\underset{\sim}{\infty}, \operatorname{diff}[\checkmark, \times])|V(\operatorname{diff}[\times, \checkmark])|!\mathcal{A}$

## Problem

State-of-the-art: $\approx$ approximated by "diff-equivalence"

```
diff-equivalence = " }\approx\mathrm{ for who knows internal structure of processes"
```

Implications:

- knows when actions are triggered by the same process/agent

Structural links given to vs. ballot privacy=absence of certain links:
$\sim$ systematic false attacks on ballot secrecy
$\sim$ ad hoc work-arounds with limited applicability e.g. swaps of processes

## Our hybrid approach: privacy via sufficient conditions

Methodology:

- focus on some class of protocols and some privacy goal
- identify conditions (inspired by generic classes of attacks)
- that are sufficient (soundness),
- fundamentally simpler and easier to check (checkability), and
- met by (secure) protocols (tightness)


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Goal: More precise \& efficient verification techniques + extends the scope.
First developed for untraceability:
L.H., D. Bælde, and S. Delaune. "A method for unbounded verification of privacy-type properties". Journal JCS'19 and conference S\&P'16.

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## Leaking Status

Take for instance: $V(\mathbb{Q}, \boldsymbol{M})=$ new $n .1$ : out $(P) \cdot P . \operatorname{cout}(\mathbb{M}) . \operatorname{out}(n)$

$$
\begin{aligned}
& \mathrm{V}=1: \begin{array}{|l|l|l|l|}
\hline \operatorname{Out}(\text { IId }) & \ln (y) & \operatorname{Out}(u) \\
\hline
\end{array} \quad \begin{array}{|l|l|l|}
\hline \operatorname{Out}(\mathbf{v}) & \operatorname{Out}(n) \\
\hline
\end{array} \\
& \begin{array}{|l|l|l}
\hline \ln (x) & \operatorname{Out}(t) & \ln (z) \\
\hline
\end{array}
\end{aligned}
$$

## Leaking Status

Take for instance: $V(\mathbb{M})=$ new $n .1$ : out $(\mathbb{C}) \cdot P \cdot o u t(\mathbb{M})$.out $(n)$


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- At most 1 type of leak in a single phase $\sim$ phase leaking status id-leaking phases unlinkable to vote $\wedge$ vote-leaking phases unlinkable to id


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- At most 1 type of leak in a single phase $\sim$ phase leaking status id-leaking phases unlinkable to vote $\wedge$ vote-leaking phases unlinkable to id
- Similarly: name has at most 1 type of leak $\leadsto$ name leaking status


## 1: Dishonest Condition

Idea: if a deviation from the honest execution at phase $i$ has some impact at phase $j>i \sim$ may link phases $i$ and $j$.
e.g. taint credential at phase 1 and observe it at phase 2

## Dishonest Condition (Informal)

For any execution, if a voter process $V$ at phase $j$ is still present at the end, then it followed the honest trace up to $j-1$.

- Prevent a class of attacks
- Allow us to focus on less executions (those that meet the condition)



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- Allow us to focus on less executions (those that meet the condition)

$$
\begin{aligned}
& \mathcal{R}^{\text {id }}\left(\mathbf{n}_{A}^{\text {id }}, \mathbf{n}_{1}^{\vee}\right)=\left\{\begin{array}{l|l|l|}
\hline 1: \operatorname{Out}(\mathbf{I}) & \ln (y) & \operatorname{Out}(u) \\
& 1: \operatorname{\operatorname {ln}(x)} & \operatorname{Out}(t) \\
\ln (z) \\
\mathcal{R}^{\vee}\left(\mathbf{n}_{A}^{\text {id }}, \mathbf{n}_{1}^{\vee}\right)=\left\{\begin{array}{l|l|l|} 
& \operatorname{Out}(\mathbf{I}) & \operatorname{Out}\left(n_{1}\right)
\end{array}\right\}
\end{array}\right.
\end{aligned}
$$

less structural links with "standalone phase-processes" ©

## 2: Relation Condition

We would like to check the absence of relation for all phase-processes. (less structural links now $)^{(\cdot)}$

$$
\operatorname{diff}\left[n_{\checkmark}^{\vee}, n_{x}^{\vee}\right] \text { in id-leaking phase-processes }
$$

Defined as the diff-equivalence of:

$$
\begin{aligned}
\mathcal{B}= & \left\{\mathcal{R}^{\text {id }}\left(\mathbf{n}_{\overparen{@}}^{\text {id }}, \operatorname{diff}\left[\mathbf{n}_{\checkmark}^{v}, \mathbf{n}_{\times}^{\mathrm{v}}\right]\right),\right. \\
& \mathcal{R}^{\text {id }}\left(\mathbf{n}_{\mathbb{C}}^{\text {id }}, \operatorname{diff}\left[\mathbf{n}_{\times}^{\mathrm{v}}, \mathbf{n}_{\checkmark}^{\mathrm{v}}\right]\right) \\
& \} \biguplus!\mathcal{R}
\end{aligned}
$$

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$$
\begin{gathered}
\operatorname{diff}\left[n_{v}^{\vee}, n_{x}^{\vee}\right] \text { in id-leaking phase-processes } \\
\operatorname{diff}\left[n_{\circlearrowleft}^{\text {id }}, n_{8}^{\text {id }}\right] \text { in vote-leaking phase-processes }
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\end{gathered}
$$

Defined as the diff-equivalence of:

$$
\begin{aligned}
& \mathcal{B}=\left\{\mathcal{R}^{\text {id }}\left(\mathbf{n}_{\Theta}^{\text {id }}, \operatorname{diff}\left[\mathbf{n}_{\sqrt{v}}^{\mathrm{v}}, \mathbf{n}_{\times}^{\mathrm{v}}\right]\right), \quad \mathcal{R}^{\vee}\left(\operatorname{diff}\left[\mathbf{n}_{\Theta}^{\text {id }}, \mathbf{n}_{\underset{\circlearrowleft}{\mathrm{id}}}^{\text {id }}\right], \mathbf{n}_{\sqrt{ }}^{\mathrm{v}}\right),\right.
\end{aligned}
$$

$$
\begin{aligned}
& \} \biguplus!\mathcal{R}
\end{aligned}
$$

## Relation Condition (Informal)

The Honest Relations Condition is satisfied if $\mathcal{B}$ is diff-equivalent.

## Our Results

Theorem (soundness)
For any $E=(V(\mathbb{M}), \mathcal{R}$, Tally), if the Dishonest, Relation, and Tally conditions hold then $E$ satisfies ballot secrecy.
(Tally condition omitted)

- We provide an algorithm for computing models checking the conditions and heuristics to find leaking status (checkability)
- We verify some case studies + benchmarks (tightness):

| Protocol | Ballot Secrecy | Our verif. time | Previous state of the art |
| :---: | :---: | :---: | :---: |
| FOO | $\checkmark$ | 0.04 | 0.26 |
| Lee 1 | $\checkmark$ | 0.04 | 46 |
| Lee 2 | $\checkmark$ | 0.05 | $\dagger$ |
| Lee 3 | $\checkmark$ | 0.01 | $\dagger$ |
| Lee 4 |  | 6.64 | 169.94 |
| JCJ | $\checkmark$ | 18.79 | $\times$ |
| Belenios | $\checkmark$ | 0.02 | $\times$ |

## Introduction

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II Application to E-Voting
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## Conclusion

## Summary

- Three tight, sufficient conditions for ballot privacy
- Expands the class of protocols and threat models that can be verified
- More efficient verification


## Future Work

- Extend our result with more precise Tally
- Combine with the new BPRIV privacy definition [S\&P'15, Euro S\&P'19]
- Provide a tool with ProVerif/Tamarin as back-end
- Reuse methodology for other contexts/privacy properties
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## Backup Slides

## Symbolic Model

Big Picture
Protocol's specification $\longmapsto$ Protocol's model


Privacy goal $\longmapsto \approx$ between scenarios


## Two Approaches for Verifying $\approx$ Automatically

Decision for $<\infty$ sessions
$<\infty$
branching


- bound the number of sessions
- symbolic semantics
$\leadsto$ finite description of
- exhaustive exploration of symbolic executions
- Tools: Apte, Akiss, Spec

Semi-decision for $\infty$ sessions


- over-approximations of \& semantics
- strong form of $\approx$ (i.e. diff-equivalence)
- Tools: ProVerif, Tamarin, Maude-NPA


## Limitation of Semi-decision Procedures



## Applied $\pi$-Calculus

Model of messages: Term algebra

- Function symbols
- Equational theory $=$ E + computation relation $\downarrow$
$\operatorname{enc}(\cdot, \cdot), \operatorname{dec}(\cdot, \cdot)$ $\operatorname{dec}(\operatorname{enc}(x, y), y) \downarrow x$

Model of protocols: Process calculus

- Process: $P, Q$ := 0 $\operatorname{in}(c, x) \cdot P$ out $(c, m) . P$
let $x=v$ then $P$ else $Q$
$P \mid Q$
$!P$
new $n . P$
$i: P$
null
input
output conditional parallel
replication
creation of name weak phase
- Frame $(\phi)$ : the set of messages revealed to

$$
\phi=\{\underbrace{w_{1}}_{\text {handle }} \mapsto \underbrace{\operatorname{enc}(m, k)}_{\text {out. message }}, w_{2} \mapsto k\}
$$

- Configuration: $A=(\mathcal{P} ; \phi ; j)$


## Applied- $\pi$ - Semantics

- Recipes: terms built using handles

$$
\begin{array}{ll}
\text { e.g. } & R=\operatorname{dec}\left(w_{1}, w_{2}\right) \quad \text { for } \quad \phi=\left\{w_{1} \mapsto \operatorname{enc}(m, k), w_{2} \mapsto k\right\}
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$$

"How builds messages from its knowledge"

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& R \phi={ }_{\mathrm{E}} m
\end{array}
$$

## "How builds messages from its knowledge"

- Protocol's output:
$(\{i: \operatorname{out}(c, u) . P\} \cup \mathcal{P} ; \phi ; i) \xrightarrow{\text { out }(c, w)}(\{i: P\} \cup \mathcal{P} ; \phi \cup\{w \mapsto u\} ; i) \quad$ if $w$ fresh
- Protocol's input:


$$
(\{i: \operatorname{in}(c, x) . P\} \cup \mathcal{P} ; \phi ; i) \xrightarrow{\operatorname{in}(c, R)}(\{i: P\{x \mapsto R \phi\}\} \cup \mathcal{P} ; \phi ; i)
$$

-     + expected rules for conditional (modulo $=_{\mathrm{E}}$ ) \& others

controls all the network


## Applied- $\pi$ - Trace Equivalence

## Static Equivalence (intuitively)

$\Phi \sim \Psi$ when

- $\operatorname{dom}(\Phi)=\operatorname{dom}(\Psi)$ and
- for all tests, it holds on $\Phi \Longleftrightarrow$ it holds on $\Psi$


## Trace Equivalence

$A \approx B$ : for any $A \xrightarrow{\mathrm{t}} A^{\prime}$ there exists $B \xrightarrow{\mathrm{t}^{\prime}} B^{\prime}$ such $\Phi\left(A^{\prime}\right) \sim \Phi\left(B^{\prime}\right)$ and $\mathrm{obs}(\mathrm{t})=\mathrm{obs}\left(\mathrm{t}^{\prime}\right)$

## Privacy

## Unlinkability

cannot establish meaningful link between two interactions (with same Id)

## Anonymity

$$
\mathcal{M} \mid \text { !new Sess. }\left(P_{x_{0}}\left(\mathrm{Id}_{0}\right) \mid P_{\infty}\left(\mathrm{Id}_{0}\right)\right) \approx ? \mathcal{M}
$$

cannot establish meaningful link between an interaction and identity $\mathrm{Id}_{0}$

## Ballot Secrecy

cannot establish meaningful link between a voter and his vote

## Goal: Analyzing Ballot Secrecy

Often, only the core voting protocol is analyzed.


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We would like to take into account important aspects such as:

- registration, credential delivery
- voting
- authentication
- tallying

We would like to:

- compare different threat models (no security if everything is compromised)
- identify minimal honesty assumptions


## Verifying Ballot Secrecy

Diff-equivalence yields false attacks
Take:

$$
V(\boldsymbol{\text { M M }} \text { ) })=1: \operatorname{out}(c, \boldsymbol{\Phi}) \cdot 2: \operatorname{out}(c, \text {, }
$$

With diff-equivalence, $\qquad$ (resp. ©)
$\sim$ attacker can link ${ }^{\ominus}$ and

## State-of-the-Art

Weakening diff-equivalence (improving the tool):

- Swapping approach - Idea:[DRS'08], Proof+ProVerif:[BB'16], Tamarin:[DDKS'17]: allows to change biprocess pairing at sync. barriers

Hybrid approaches:

- type system [CGLM'17]
- small attack property [ACḰ16]


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- no swap/phase under replication $\sim$
- no honest authority present in $\neq$ phases
- no threat model with no dishonest voters
- introduction of new internal communication $\sim$
- false attacks in presence of fresh data going through phases ( 1 : new $n .2: \operatorname{out}(c,(v, n)$ )

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Hybrid approaches:

- type system [CGLM'17] but pairing is as rigid as diff-equivalence, standard primitives only
- small attack property [ACK'16] but only 1 phase, performance issues

In practice, interesting threat models and modeling of e.g. Lee, JCJ, Belenios are out of the scope

## Our contribution - Big Picture

We develop a privacy via sufficient conditions approach for ballot secrecy and a large class of e-voting protocols (soundness, checkability, tightness).

We apply our technique on FOO, Lee, JCJ and Belenios (with registration):

- false attacks using previous techniques
- much better performance
(e.g. JCJ, Belenios)
(e.g. $* 10^{2}$, termination for LEE)


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- much better performance
(e.g. $* 10^{2}$, termination for LEE)

Main Limitation:

- Tallier is too unrealistic: no revote policy, homomorphic tallying


## Class of e-voting protocols

(Honest) Roles:

- Voter: $V(\mathbb{M})=i$ : new $\vec{n} . V^{\prime}$ such that $V^{\prime}$ has no !, | or new
- $A \in \mathcal{R}$ authority session, same format $+(?)$ voters
- Some role $A_{c} \in \mathcal{R}$ is the bulletin box and $A_{b} \ni \operatorname{out}\left(c_{b}, t\right)$

Tally:

- Made of a public term $\Psi_{b}$ (correct form?) and private term Extract (check validity and extract vote)
- "Tally" $=!i_{f}: \operatorname{in}(c, x)$.let $\left(\_, v\right)=\left(\Psi_{b}[x]\right.$, Extract $\left.[x]\right)$ in out $(c, v)$

Honest Trace: (symbolic) trace th s.t. $\left(\mathcal{R} \cup\{V(\varnothing, \checkmark)\} ; \phi_{0} ; 1\right) \xrightarrow{\text { th }}\left(\varnothing ; \phi ; i_{f}\right)$

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E-Voting Protocol:

$$
\left(\mathcal{V} ; \phi_{0} ; V(\mathbb{\Theta}, \underline{M}), \mathcal{R},\left(\Psi_{b}, \text { Extract }\right)\right)
$$

## Ballot Secrecy

## (Weak) phases are not enough

Take:
$V(\mathbb{M})=1: \operatorname{out}(c, \boldsymbol{Q}) \cdot 2: \operatorname{out}(c$, , $)$

But strong phases suffer from theoretical limitations w.r.t. replications. Idea:

- Executions with strong phases = executions with weak phases that wait for all processes at each phase jump


## Ballot Secrecy



## (Weak) phases are not enough

Take:


But strong phases suffer from theoretical limitations w.r.t. replications. Idea:

- Executions with strong phases = executions with weak phases that wait for all processes at each phase jump
- Fair executions = executions with weak phases that wait for and

Ballot Secrecy: Use weak phases $+\approx$ fair instead of strong phases $+\approx$

## Leaking Status

$$
\begin{aligned}
& \mathrm{V}=1: \begin{array}{|l|l|l|l|}
\hline \operatorname{Out}(\mathbf{I}(\mathbf{l}) & \ln (y) & \operatorname{Out}(u) \\
\hline
\end{array} \quad \begin{array}{|l|l|l|}
\hline \operatorname{Out}(\mathbf{z}) & \operatorname{Out}(n) \\
\hline
\end{array} \\
& \mathrm{A}=1: \begin{array}{|l|l|l|}
\hline \ln (x) & \operatorname{Out}(t) & \ln (z) \\
\hline
\end{array}
\end{aligned}
$$

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- at most 1 type of leak in a single phase $\leadsto$ phase leaking status
id-leaking phases unlinkable to $v$ $\wedge$ vote-leaking phases unlinkable to id $\approx\binom{$ diff $\left[v_{1}, v_{2}\right]$ in id-leaking phases }{ diff $\left[i d_{1}, i d_{2}\right]$ in vote-leaking phases }


## Leaking Status



- at most 1 type of leak in a single phase $\sim$ phase leaking status id-leaking phases unlinkable to $v$ $\wedge$ vote-leaking phases unlinkable to id $\approx\binom{\operatorname{diff}\left[v_{1}, v_{2}\right]$ in id-leaking phases }{$\operatorname{diff}\left[i d_{1}, i d_{2}\right]$ in vote-leaking phases }
- name has at most 1 type of link $\sim$ name leaking status id-leaking phases/names unlinkable to $v$
vote-leaking phases/names unlinkable to id $\quad \approx\binom{\operatorname{diff}\left[\mathbf{n}_{1}^{v}, \mathbf{n}_{2}^{v}\right]$ in id-leaking phases }{$\operatorname{diff}\left[\mathbf{n}_{1}^{i d}, \mathbf{n}_{2}^{i d}\right]$ in vote-leaking phases }


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But diff-equivalence is still problematic

## Phase-Process and Dishonest Condition

Idea: if a deviation from the honest execution in phase $i$ has some impact in phase $j>i \sim$ may link phases $i$ and $j$.
e.g. "weaken"/taint credential in phase 1 and observe it in phase 2

Dishonest Condition (Informal)
For any fair execution $\left(\mathcal{S} ; \phi_{0} ; 1\right) \xrightarrow{\text { t.phase }(j)}(\mathcal{P} ; \phi ; j)$, if a process at phase $j$ annotated $[\mathcal{Q}, \mathbb{Z}]$ for $\in\{\mathbb{Q}\}$ and $\mathcal{V}$ is present in $\mathcal{P}$ then it followed th up to phase $j$.

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- Prevent a class of attacks
- Allow us to focus on less executions (those that meet the condition)

$$
\begin{aligned}
& \mathrm{V}=1: \begin{array}{l|l|l|l|l|}
\hline \operatorname{Out}(\text { Ita) } & \ln (y) & \operatorname{Out}(u) & \text { Out(I) } & \operatorname{Out}(n) \\
\mathrm{A}=1: & \ln (x) & \operatorname{Out}(t) & \ln (z)
\end{array}
\end{aligned}
$$

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$$
\begin{aligned}
& \mathcal{R}^{\text {id }}\left(\mathbf{n}_{A}^{\text {id }}, \mathbf{n}_{1}^{v}\right)=\left\{\begin{array}{l|l|l|l|}
1: & \operatorname{Out}(\mathbf{L}) & \ln (y) & \operatorname{Out}(u) \\
1: & \ln (x) & \operatorname{Out}(t) & \ln (z)
\end{array}\right\} \\
& \mathcal{R}^{\vee}\left(\mathbf{n}_{A}^{\text {id }}, \mathbf{n}_{1}^{v}\right)=\left\{\begin{array}{l|l|l}
2: & \operatorname{Out}(\mathbf{I}) & \operatorname{Out}\left(n_{1}\right)
\end{array}\right\}
\end{aligned}
$$

## Relation Condition

We would like to check the absence of relation for all phase-processes. (less structural links now ©)

$$
\begin{aligned}
& \operatorname{diff}\left[n_{V}^{\vee}, n_{x}^{v}\right] \text { in id-leaking process-phases } \\
& \operatorname{diff}\left[n_{s}^{\text {id }}, n_{\frac{i d}{i d}}^{\text {id }}\right] \text { in vote-leaking process-phases }
\end{aligned}
$$

Formally defined through a bi-process:

$$
\begin{aligned}
& \left.\biguplus!\mathcal{R} ; \phi_{0} ; 1\right)
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$$

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\begin{aligned}
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& \operatorname{diff}\left[n_{ভ}^{\text {id }}, n_{\frac{i d}{\text { id }}}\right] \text { in vote-leaking process-phases }
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## Relation Condition (Informal)

The Honest Relations Condition is satisfied if $\mathcal{B}$ is diff-equivalent and th is phase-oblivious.
th is phase-oblivious when it dœs not connect a handle and a recipe of different leaking status

## Tally Condition

Goal: prevents ballot secrecy attacks that exploit the tally's outcome. Ballots are either:

1. (honest): stems from an honest execution of or
2. (dishonest): dœs not depend on data that can be linked to an identity
$\sim$ the vote Tally would extract is insensible to the swap $\leftrightarrow$

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## Tally Condition (Informal)

$\forall$ fair execution $\mathcal{B} \xrightarrow{\mathrm{t}}\left(\mathcal{P}^{\prime},\left(\phi_{l}, \phi_{r}\right)\right)$, for any ballot $w \phi_{l}$ in the BB , either:

1. there exists a voter $V(\mathbb{Q}, \mathbb{Q}),\{\in\}$ who had an honest interaction and who has cast $w$
2. or there exists some $v \in \mathcal{V} \cup\{\perp\}$ such that $\operatorname{Extract}\left(w \phi_{l}\right) \downarrow v$ and Extract $\left(w \phi_{r}\right) \downarrow v$.

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3. Ballot can depend on data from vote-leaking phases but not from id-leaking phases
$\sim$ bias leaking information on a ballot unlinkable to or is ok
$\sim$ refines ballot independence

## Our Results

Theorem (soundness)
For any $E=\left(\mathcal{V} ; \phi_{0} ; V(\mathcal{Q}), \mathcal{R},\left(\Psi_{b}\right.\right.$, Extract $\left.)\right)$, if the Dishonest, Relation and Tally conditions hold then $E$ satisfies ballot secrecy.

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- We provide an algorithm for computing models checking the conditions and heuristics to find leaking status (checkability)
(tool is FW)
- We apply our techniques to several case studies and compare ourselves with the swapping technique (tightness):

| Protocol | Ballot Secrecy | Our verif. time | Swapping technique verif. time |  |
| :--- | :---: | :---: | :--- | :--- |
| FOO | $\checkmark$ | 0.04 | 0.26 |  |
| Lee 1 | $\checkmark$ | 0.04 | 46 | (collapsed-phases: 45.33) |
| Lee 2 | $\checkmark$ | 0.05 | $\dagger$ | (collapsed-phases: 269.06) |
| Lee 3 | $\checkmark$ | 0.01 | $\dagger$ |  |
| Lee 4 | $\times$ | 6.64 | 169.94 |  |
| JC | $\checkmark$ | 18.79 | $\times$ |  |
| Belenios | $\checkmark$ | 0.02 | $\times$ |  |

## Conclusion

## Reusing core ideas

- Adapt for the case of receipt-freeness and cœrcion-resistance
- Reuse methodology for other contexts/privacy properties
- Infer generic framework (e.g. separation btw. data and active deviation issues)
- Extract guidelines for privacy from our conditions (?)


## Future Work

- Extend our result with more precise Tally:
- Combine with the new BPRIV privacy definition [S\&P'15, Euro S\&P'19]
- Provide a tool with ProVerif/Tamarin as back-end
- Reuse methodology for other contexts/privacy properties

